



# TumbleBit: An Untrusted Bitcoin-Compatible Anonymous Payment Hub

Ethan Heilman, Leen AlShenibr, Foteini Baldimtsi,  
Alessandra Scafuro, Sharon Goldberg



Scaling Bitcoin Milan 2016



# Introduction

## TumbleBit is:

1. **Private:** Unlinkable Bitcoin payments and k-anonymous mixing,
2. **Untrusted:** No one including Tumbler can steal or link payments.
3. **Scalable (payment hub):** scales transaction velocity and volume.
4. **Compatible:** Works with today's Bitcoin protocol.

## Why is compatibility hard?

Our protocol must work with highly constrained Bitcoin scripts which provide two very limited cryptographic operations.

## Two ways to use TumbleBit:



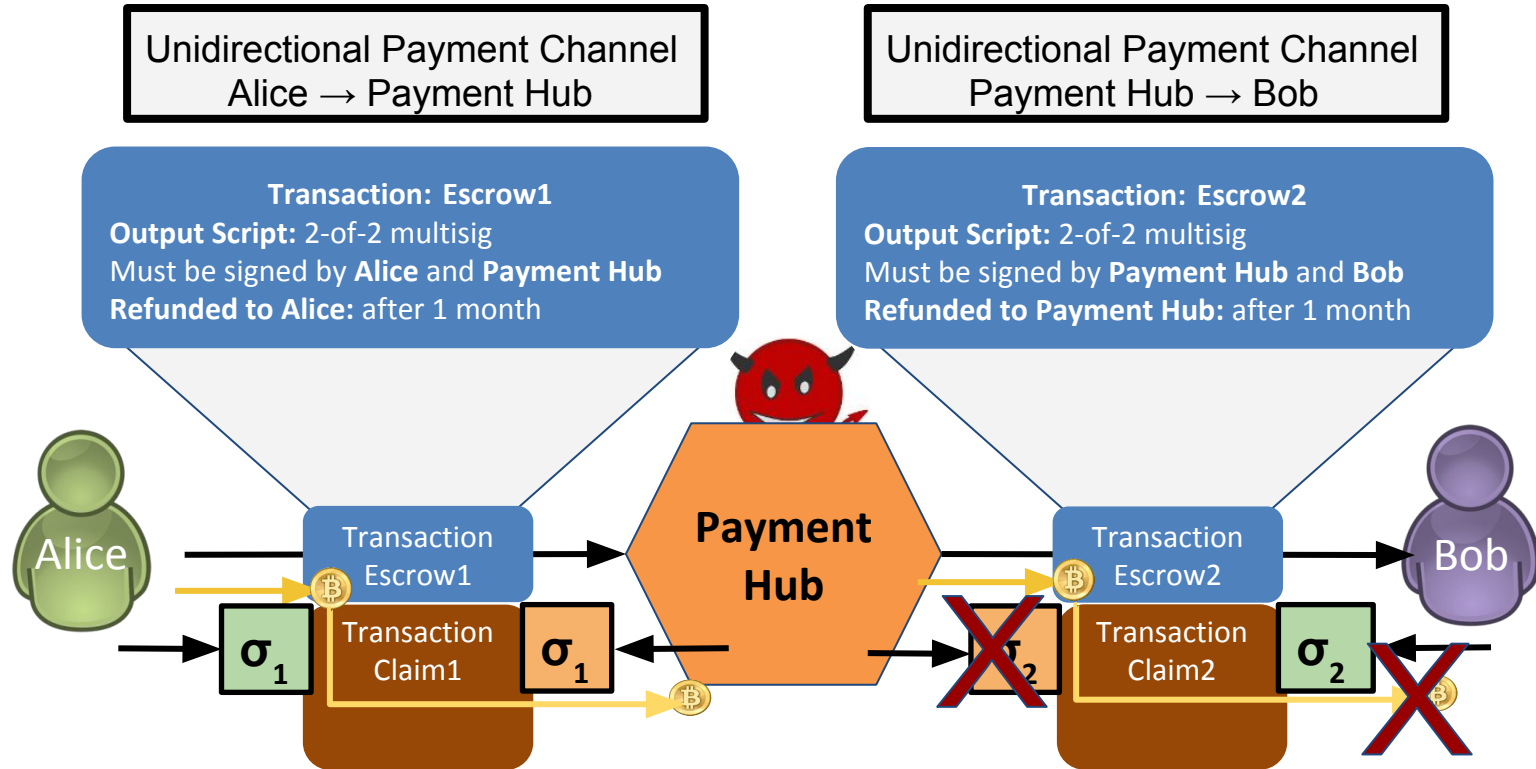
When used as a payment hub, TumbleBit helps scale Bitcoin's transaction velocity (faster payments), and transaction volume (higher maximum payments).

### When TumbleBit is used as a payment hub:

- Unlinkability within the payment phase,
- Payments confirmed in seconds,
- Payments are off-blockchain,  
... don't take up space on the blockchain.

# Background: Payment Hub

**A payment hub:** routes payment channels.



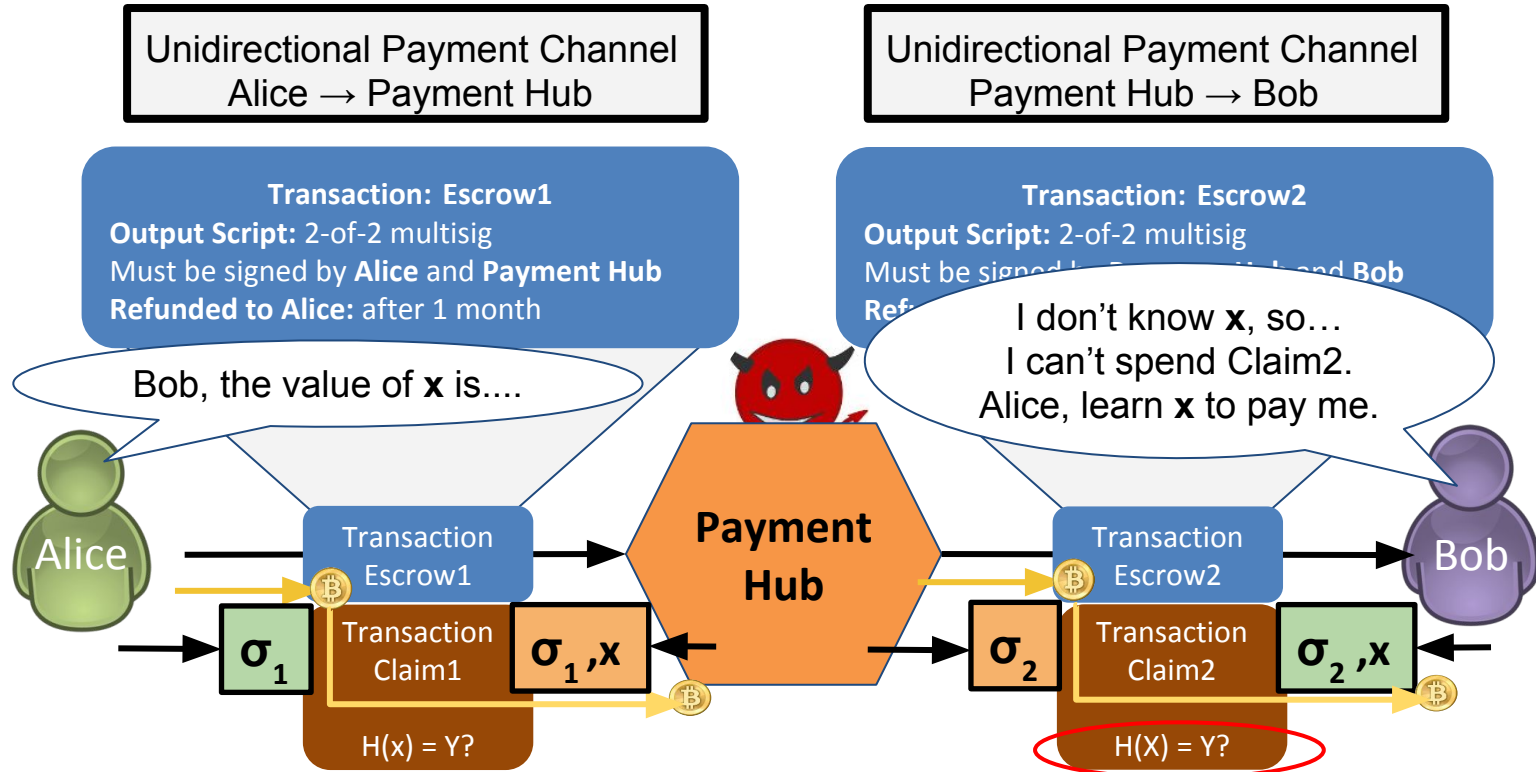
**...But what if the hub is malicious,**

**Atomicity:** If Claim1 and Claim2 happen atomically then theft is prevented.

Hash locks provide this property.

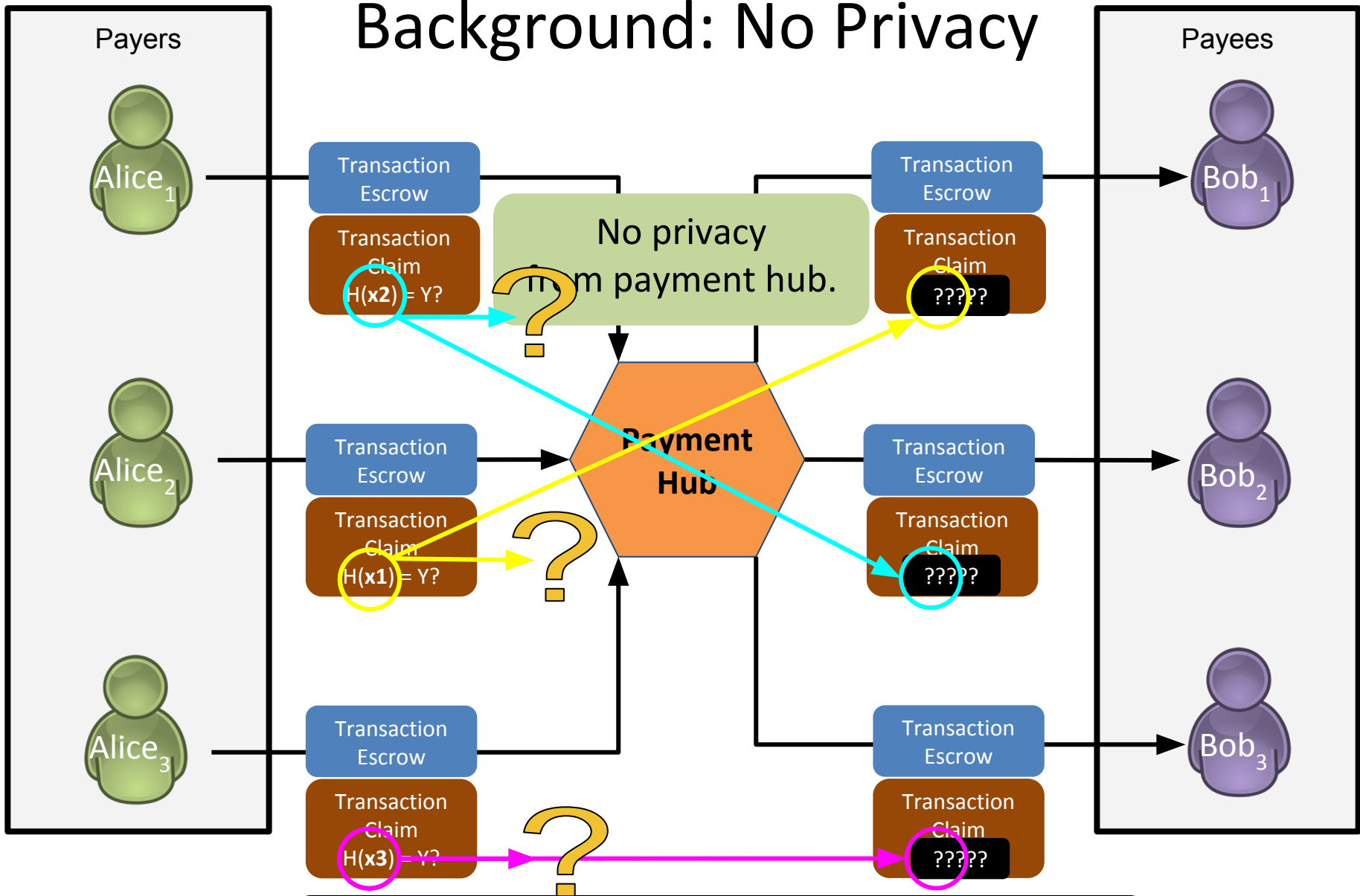
# Background: Payment Hub

A payment hub: routes payment channels.



**Thus,** using hash locked transactions or HTLCs a payment hub can prevent theft, however this provides no privacy against the payment hub.

# Background: No Privacy

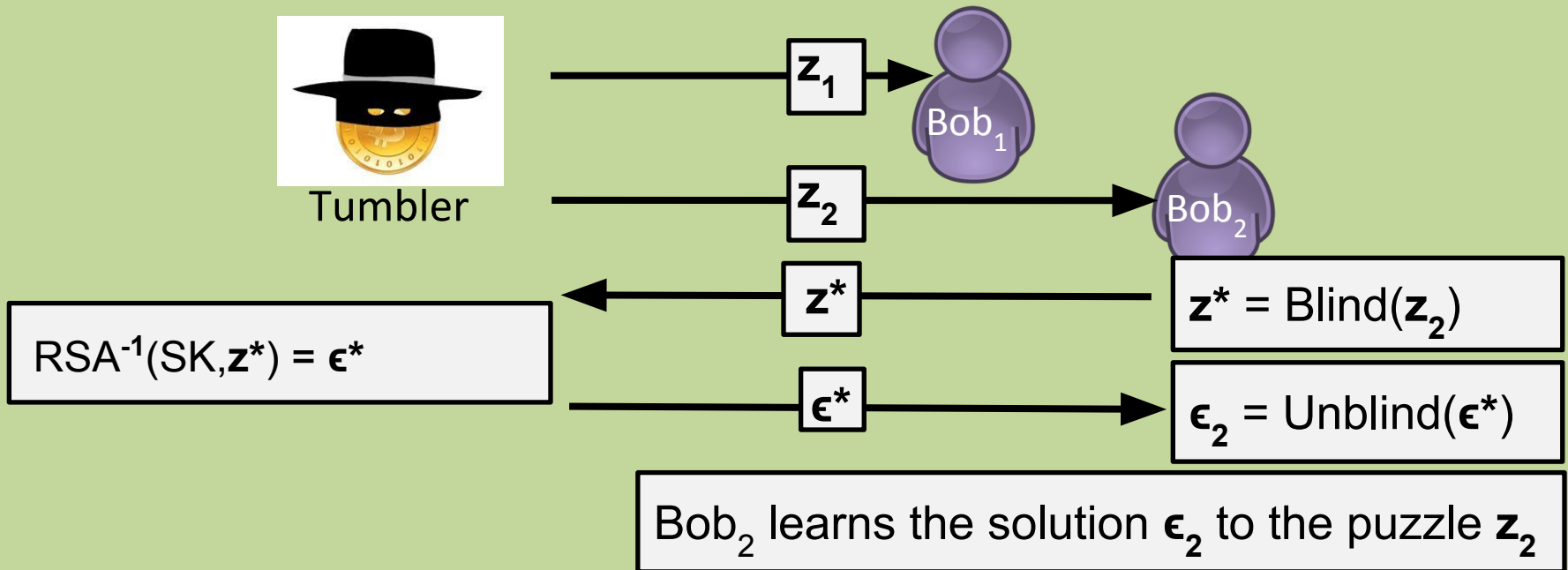


The main idea behind TumbleBit is a protocol which provides **atomicity** but is also **unlinkable** (i.e. private). Think of it like Unlinkable or Private HTLCs.

# RSA Puzzles

- An RSA Puzzle is just a “textbook RSA encryption” of some value  $\epsilon$ :  
$$\text{RSA}(\text{PK}, \epsilon) = z$$
- Only the party that knows SK can solve RSA puzzles:  
$$\text{RSA}^{-1}(\text{SK}, z) = \text{RSA}^{-1}(\text{SK}, \text{RSA}(\text{PK}, \epsilon)) = \epsilon$$

**RSA blinding can be used to blind RSA puzzles**

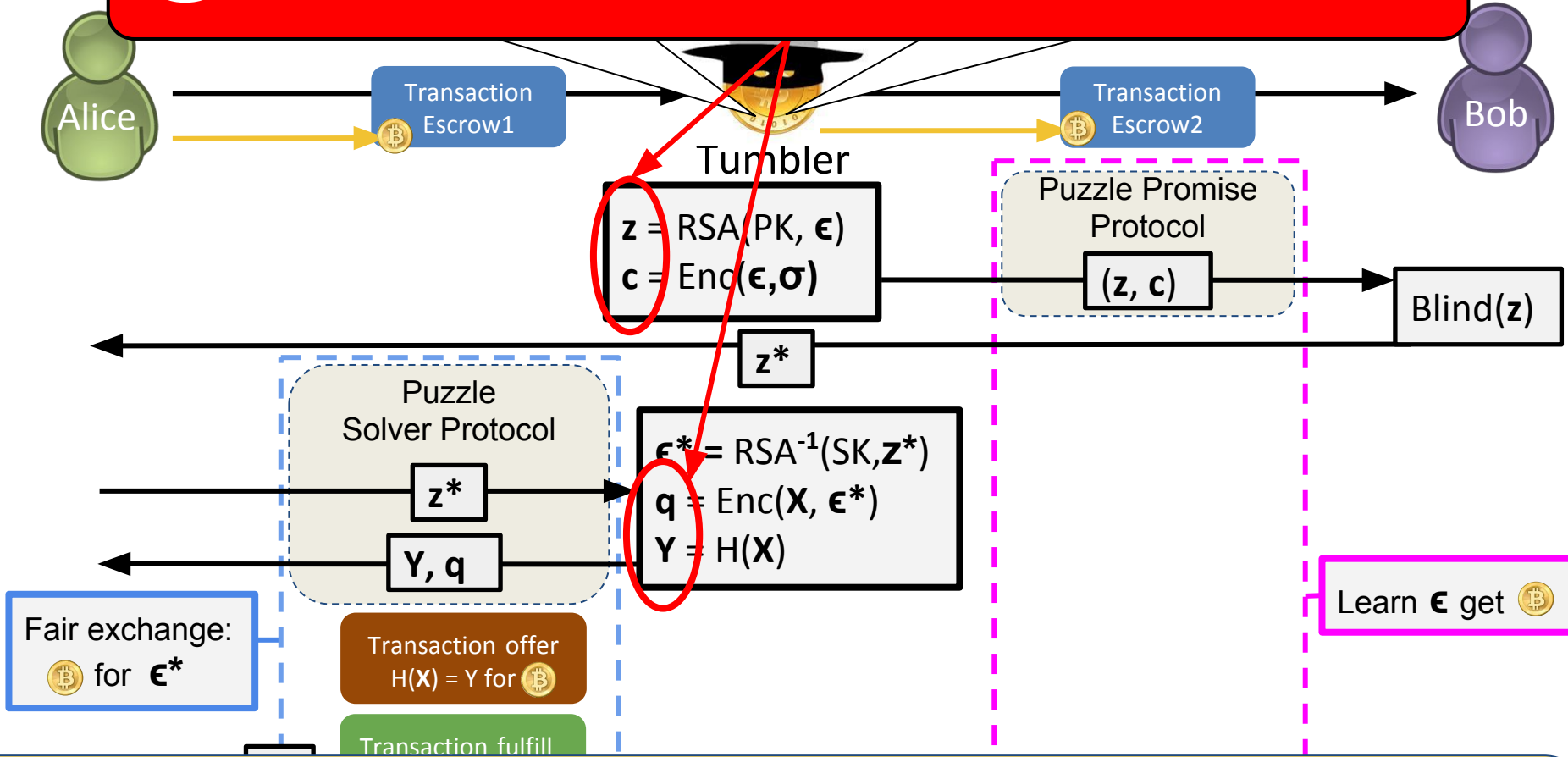


Tumbler can not link the blinded RSA puzzle it solves  $z^*$  to any of the RSA puzzles it issued ( $z_1, z_2$ ).

# TumbleBit: Protocol Overview



If Tumbler corrupts  $z$ ,  $c$ ,  $X$ , or  $q$  it can cheat Alice or Bob!



TumbleBit prevents this via two protocols:

## Puzzle-Solver-Protocol:

Tumbler convinces Alice the preimage  $X$  where  $\text{Hash}(X) = Y$  will allow her to learn  $\epsilon^*$ .

## Puzzle-Promise-Protocol:

Tumbler convinces Bob that the solution to RSA puzzle  $z$  is a value  $\epsilon$  which allows him learn  $\sigma$ .

# TumbleBit: Phases

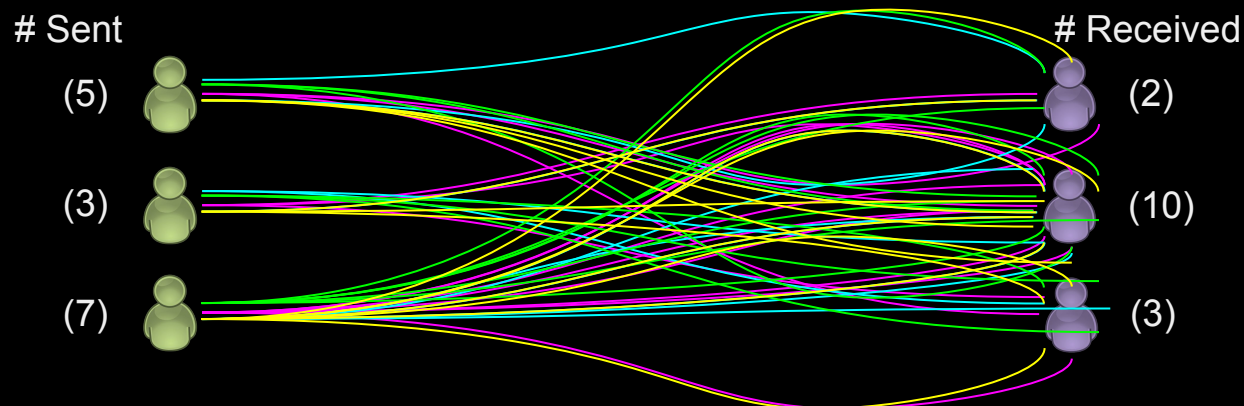
## Privacy offered the TumbleBit Payment Hub

### Tumbler's view:

(1) payer of each payment, (2) # of payments each payee received.

### Unlinkability def:

All interaction graphs compatible with the tumblers view are equally likely.

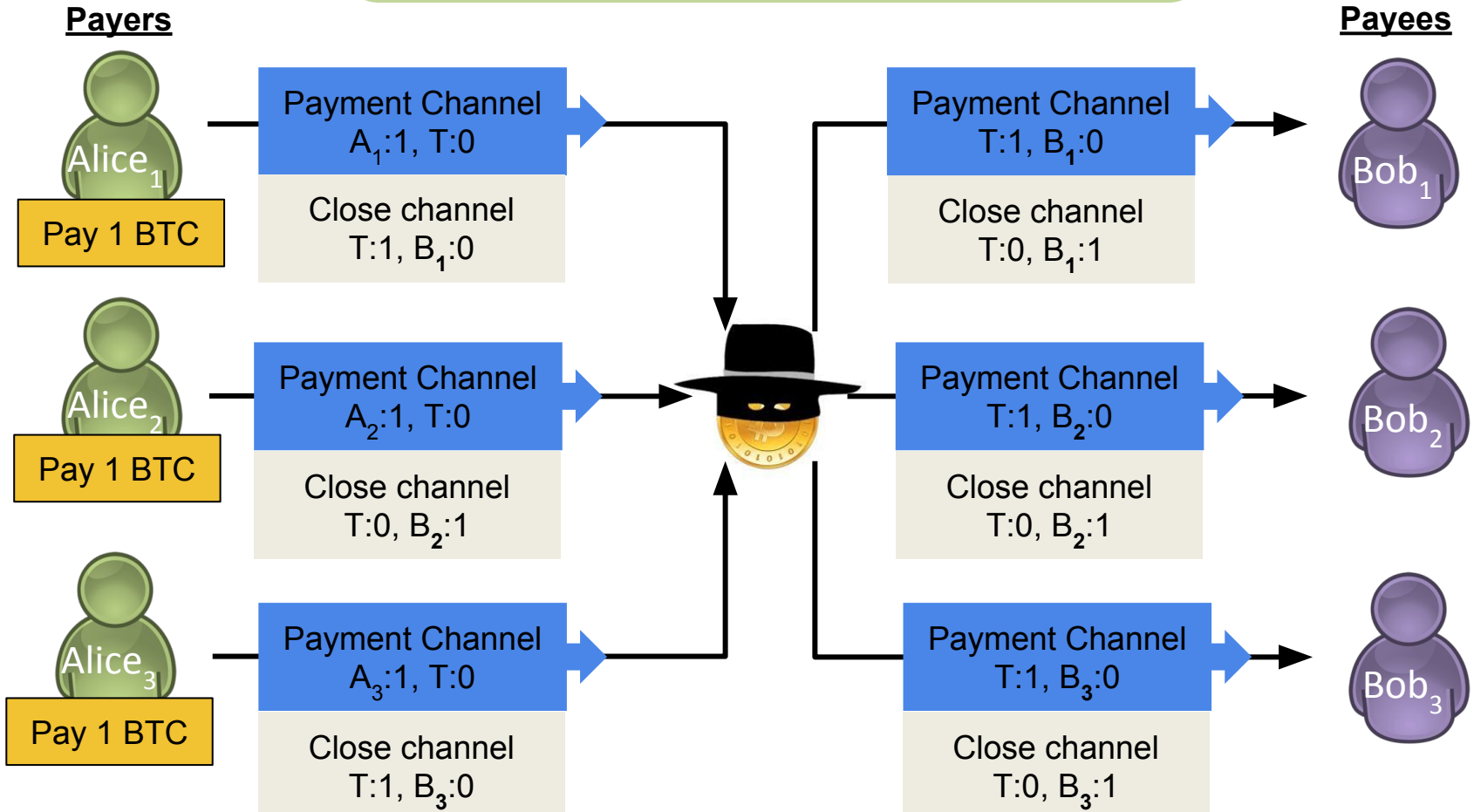




# TumbleBit: Classic Tumbler

To run TumbleBit as a Classic Bitcoin Tumbler:

- Each payer just makes one payment.
- Each payee accepts only one payment.
- # of payers = # of payees.



**Provides k-anonymity:**

Where  $k = \# \text{ of payers} = \# \text{ of payee}$ .

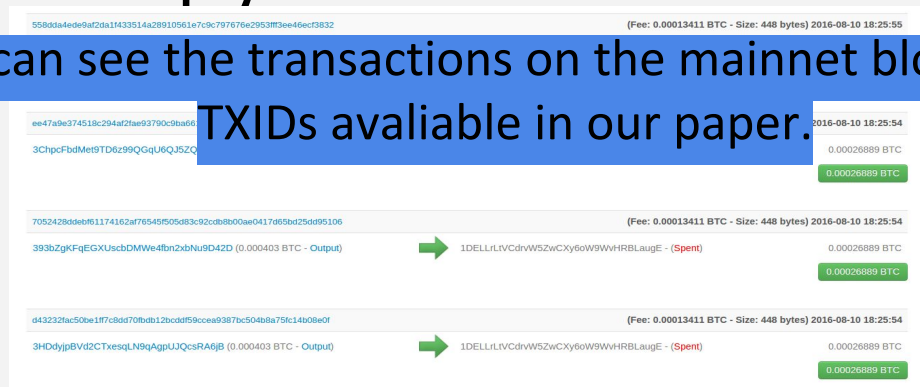
# TumbleBit: Implementation

We wrote a proof-of-concept implementation of the Tumbler mode:

- We are working on improving it and making it user friendly.
- Sourcecode and a development roadmap are available on Github.

We “tumbled” 800 payments:

You can see the transactions on the mainnet blockchain.  
TXIDs available in our paper.



Our implementation is Performant (per TumbleBit payment):

- 326 KB of Bandwidth,
- Puzzle-Solver takes ~0.4 seconds to compute
- Total time depends on network latency:  
No latency ~0.6 seconds.  
Boston to Tokyo ~6 seconds(clear) and ~11 seconds(both parties user TOR)

# Related Work

## New Cryptocurrencies

Not compatible with bitcoin



## Bitcoin-Compatible Schemes

(aka "Mixing Services")

Vulnerable to bitcoin theft



MIXCOIN  
True Anonymous Cryptocurrency

Blindcoin:



Vulnerable to DoS & Sybil Attacks



Limited Anonymity

CoinShuffle



Intermediary  
breaks  
anonymity

Mixing takes  
hours

Xim

TumbleBit

# Conclusion

**TumbleBit provides:  
private untrusted scalable payments via today's Bitcoin:**

1. **Private:** Unlinkable or k-anonymous payments
2. **Trustless:** Tumbler can not steal or link payments.
3. **Scalable (payment hub):** scales Bitcoin's transaction velocity and volume.

**We have running code (for TumbleBit classic tumbler):**

- Our code runs on Bitcoin's mainnet blockchain.
- We have published our code on github..
- ...and we working to improve it and make TumbleBit easy and safe to use.

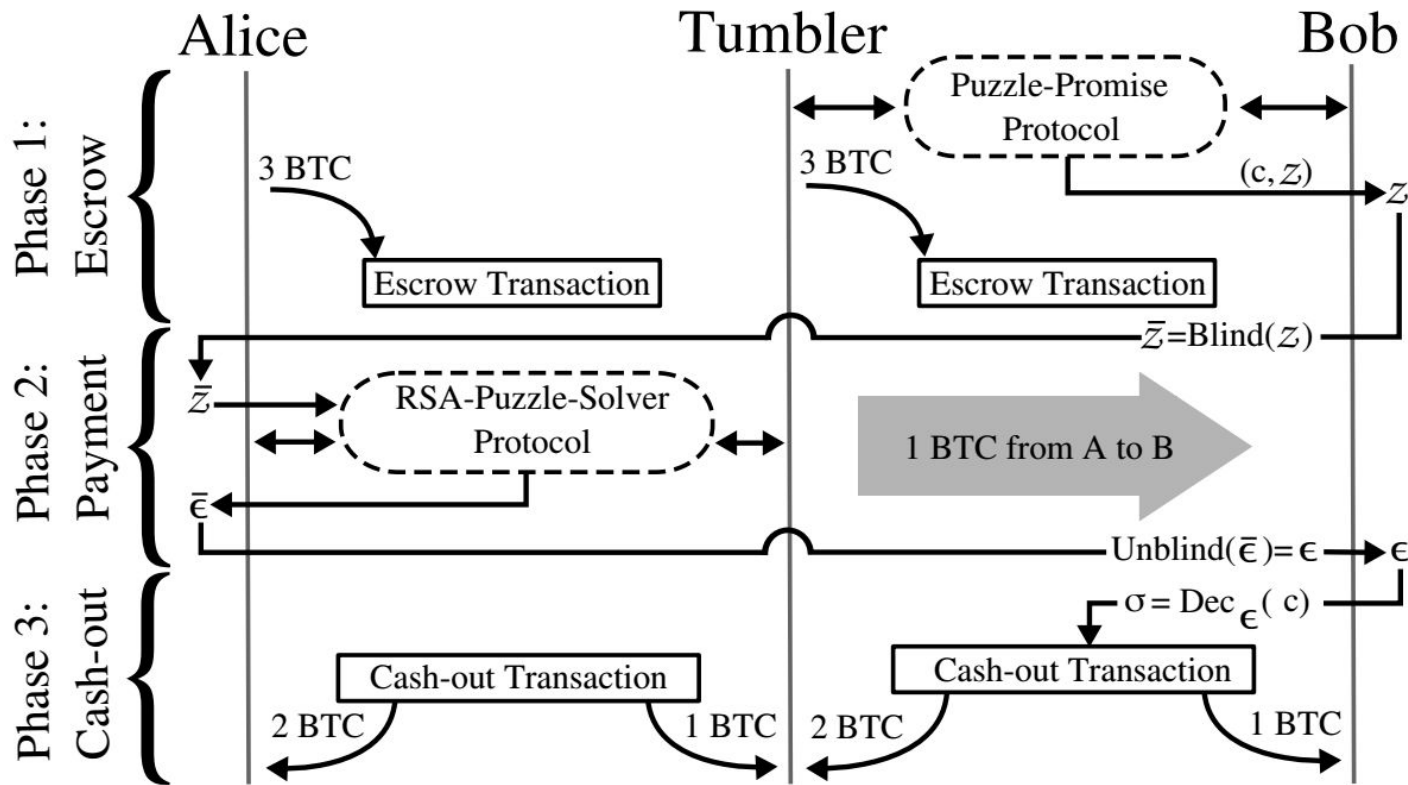


We are hiring a full time engineer (Boston),  
email me if interested.

# Questions?

Source code + roadmap: <https://github.com/BUSEC/TumbleBit>

Paper: <https://eprint.iacr.org/2016/575.pdf>



Ask questions on twitter: @Ethan\_Heilman

# TumbleBit: Puzzle-Solver-Prot

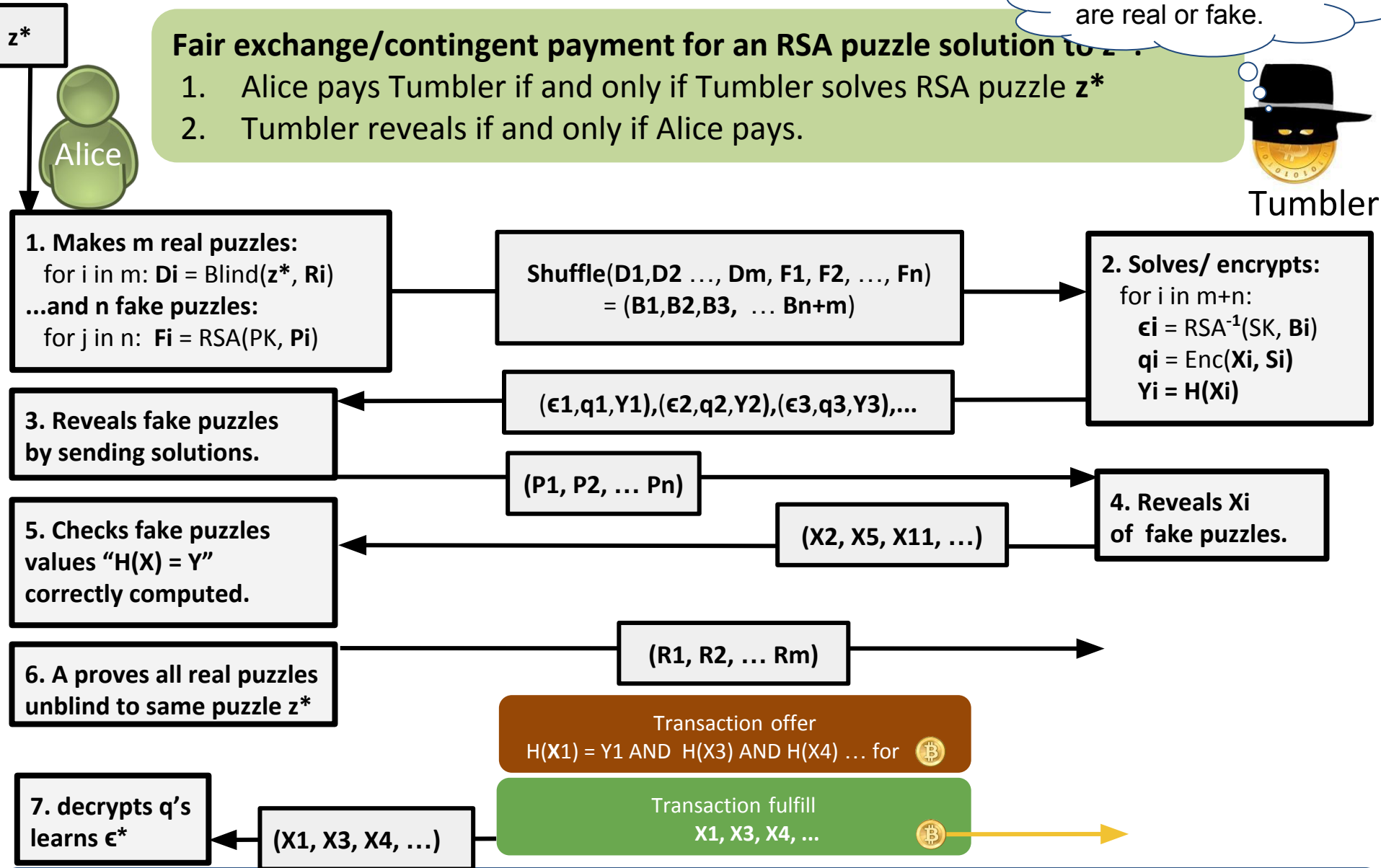
I can't tell which B's are real or fake.

Fair exchange/contingent payment for an RSA puzzle solution to  $z^*$ .

1. Alice pays Tumbler if and only if Tumbler solves RSA puzzle  $z^*$
2. Tumbler reveals if and only if Alice pays.



Tumbler



If Tumbler computes any  $(q_i, \epsilon_i, Y_i)$  of the real puzzles correctly Alice learns  $\epsilon^*$ , thus to cheat Alice, Tumbler must corrupt all the real and none of the fake puzzles.

# TumbleBit: Puzzle-Promise-Protocol

At the end of this protocol: Bob should be convinced that for a  $(z, c)$ :

1. The ciphertext  $c$  decrypts to  $\sigma$  under a key  $\epsilon$  i.e  $\text{Dec}(\epsilon, c) = \sigma$
2. AND the key  $\epsilon$  is the solution to the RSA-puzzle  $z$ .

The protocol should never: allow Bob to learn a valid  $\sigma$  (without paying).



1. B sends: a mix of hashes of valid and invalid claim transactions.

$B = H(T1), H(\text{invalid}), H(\text{invalid}), H(T4), H(\text{invalid}), H(T6)$

2. T Signs & Encrypts  $\sigma$ :  
for  $B_i$  in  $B$ :  
 $\sigma_i = \text{Sig}(\dots)$   
 $z_i = \text{RS}(\dots)$

This is why the protocol is hard,  
otherwise Tumbler could convince Bob

Probability(Tumbler successfully cheats) =  $(m+n \text{ choose } m) = \sim 1/(2^{80})$   
 $m = \#$  of valid transactions = 15  
 $n = \#$  of invalid transactions = 285

4. T Reveals:  $\epsilon_i$  for invalid transactions.

$\epsilon_2, \epsilon_3, \epsilon_5$

3. B checks: invalid transactions  $\sigma_i$  are correctly computed.

6. Bob and Tumbler run "quotient protocol" ensuring that:  
if Bob learns  $\epsilon_1$ , Bob can use that knowledge to learn  $\epsilon_4, \epsilon_6$ .  
 $(\epsilon_4/\epsilon_1 \text{ mod } N, \epsilon_6/\epsilon_4 \text{ mod } N)$

If Tumbler computes any  $(\epsilon_i, \sigma_i)$  of the valid transactions correctly Bob learns a  $\sigma$ /gets paid, thus to cheat Bob, Tumbler must all corrupt all the valid and none of the invalid transactions.

# TumbleBit: Future Roadmap

## People want TumbleBit...

Ethan ✪ Heilman @Ethan\_Heilman · Aug 29

4,943

New version of TumbleBit rewritten to focus on anonymity of #Bitcoin payment hubs/micropayment channels: [eprint.iacr.org/2016/575](http://eprint.iacr.org/2016/575) #privacy

C++ ★ 42

[View Tweet activity](#)

**but to get TumbleBit into the hands of everyday users we need to build  
...secure, safe, and usable software.**

### Phase 1: Code Safety and Testing

- ☐ Move as much code as possible into python for improved memory safety.
- ☐ Modularize code to allow our core protocol to be used in other settings.
- ☐ Replace openssl-ECDSA with libsecp256k1.

### Phase 2: Server Features

- ☐ Payment Hub support.
- ☐ Misbehavior reactive server and client.
- ☐ Session Management and parallelization.
- ☐ TOR integration.
- ☐ Standardized REST Interface.

### Phase 3: Usability and Wallets

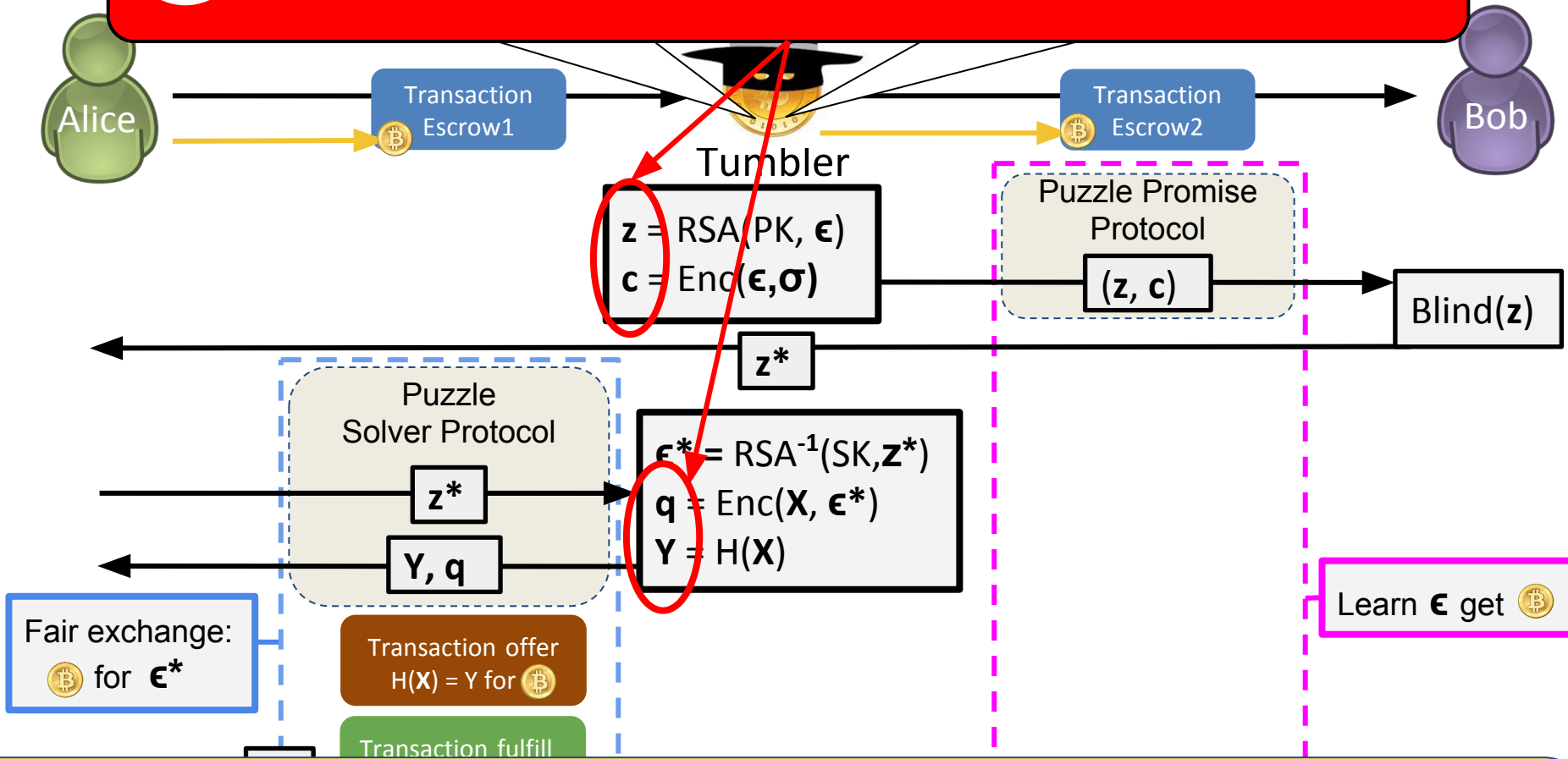
- ☐ Wallet Prototype.
- ☐ Classic Tumbler Wallet integration.
- ☐ Payment Hub Wallet integration.
- ☐ Wallet to wallet demo.



# TumbleBit: Protocol Overview



If Tumbler corrupts  $z$ ,  $c$ ,  $X$ , or  $q$  it can cheat Alice or Bob!



TumbleBit prevents this via two protocols:

## Puzzle-Solver-Protocol:

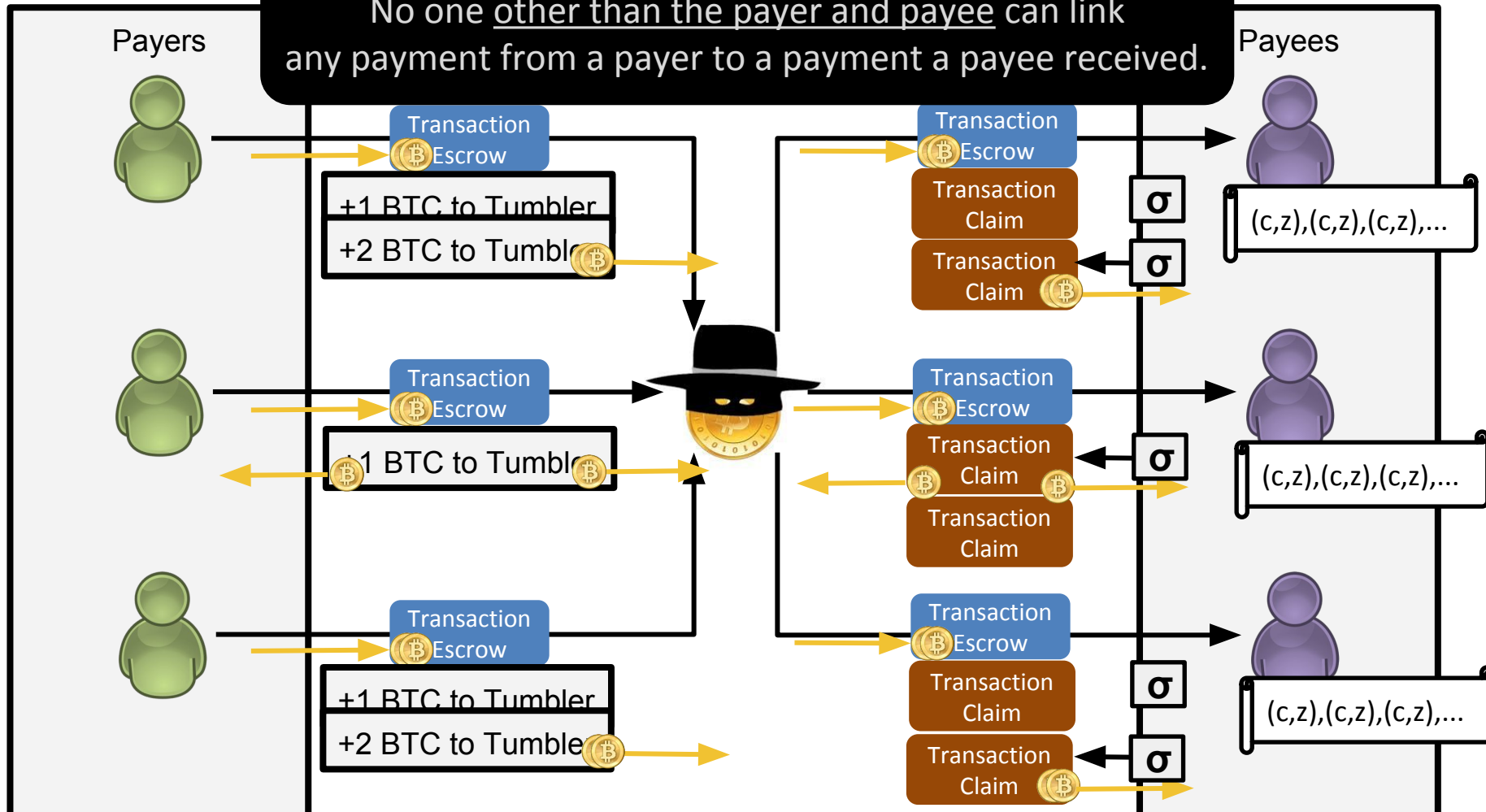
Tumbler convinces Alice the preimage  $X$  where  $\text{Hash}(X) = Y$  will allow her to learn  $\epsilon^*$ .

## Puzzle-Promise-Protocol:

Tumbler convinces Bob that the solution to RSA puzzle  $z$  is a value  $\epsilon$  which allows him learn  $\sigma$ .

# TumbleBit: Privacy

**Payments are unlinkable:**  
No one other than the payer and payee can link any payment from a payer to a payment a payee received.

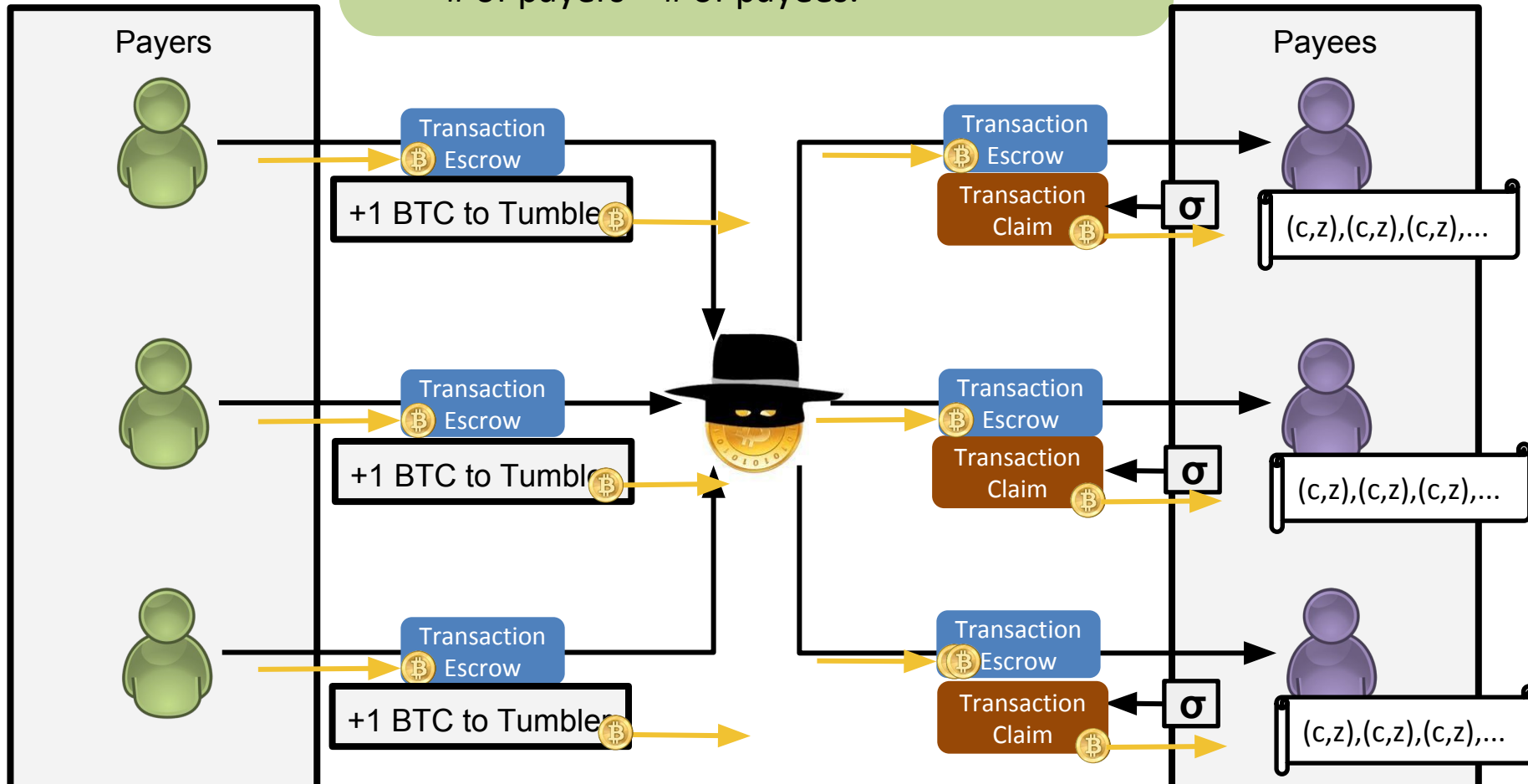


**Tumbler learns:** (1) payer & time of payment, (2) # of payments each payee received.

# TumbleBit: Classic Tumbler

To run TumbleBit as a Classic Bitcoin Tumbler:

- Each payer just makes one payment.
- Each payee accepts only one payment.
- # of payers = # of payees.



**Provides k-anonymity:**

Where  $k = \# \text{ of payers} = \# \text{ of payee}$ .

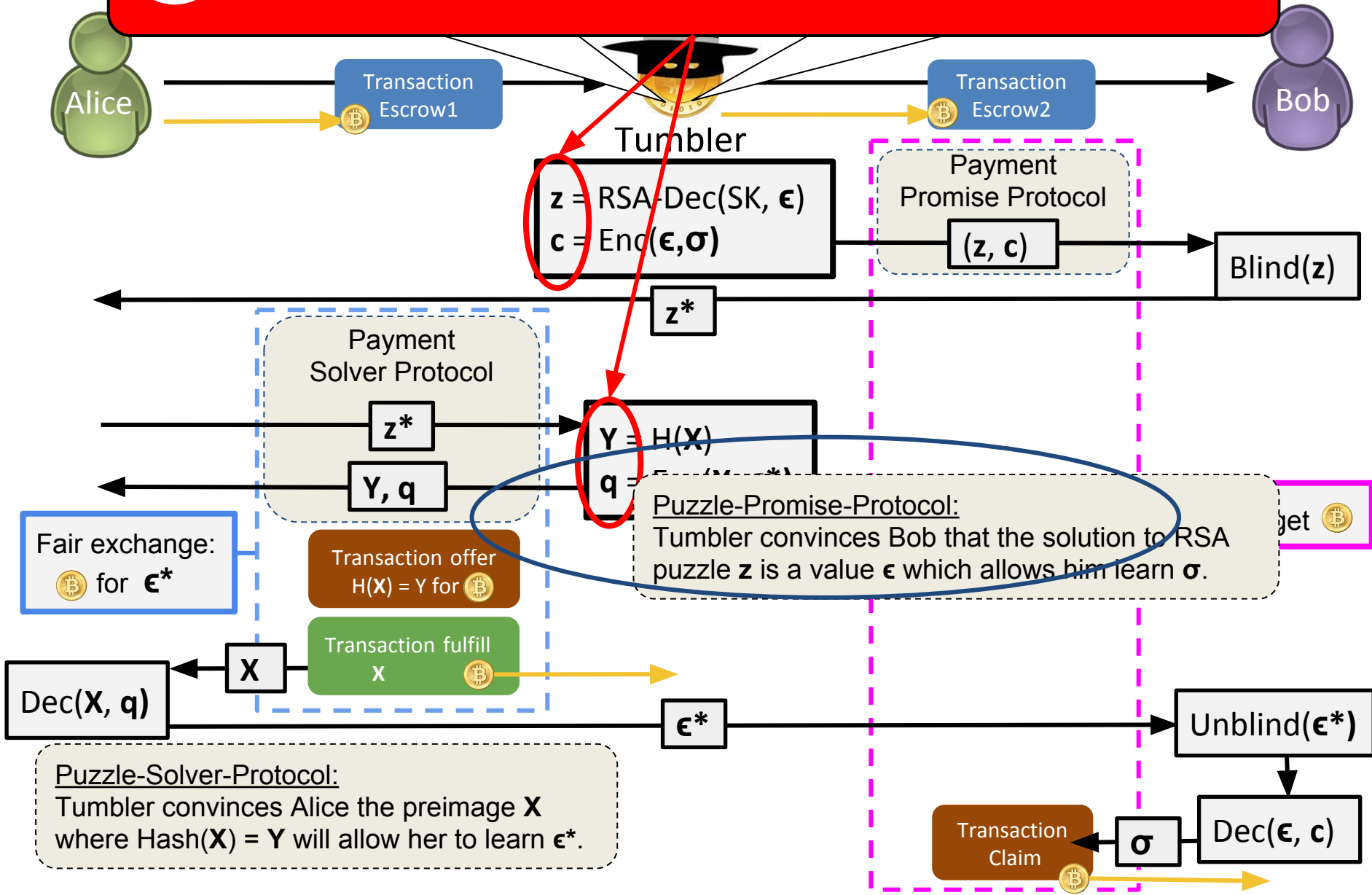
# TumbleBit: Implementation

- 1. We wrote a proof-of-concept implementation:**
  - Source code is available on Github.
  - We are working to improve it to make it user ready.
- 2. We “tumbled” 800 addresses to 800 addresses:**
  - In our paper we provide links to runs on Bitcoin’s blockchain (mainnet).
- 3. Our implementation is Performant:**
  - 326 KB of Bandwidth.
  - Computation time 0.3 - 0.6 seconds.
  - Total time depends on network latency:
    - No latency ~0.6 seconds.
    - Boston to NYC ~1.6 seconds.
    - Boston to Tokyo ~ 4.18 seconds.

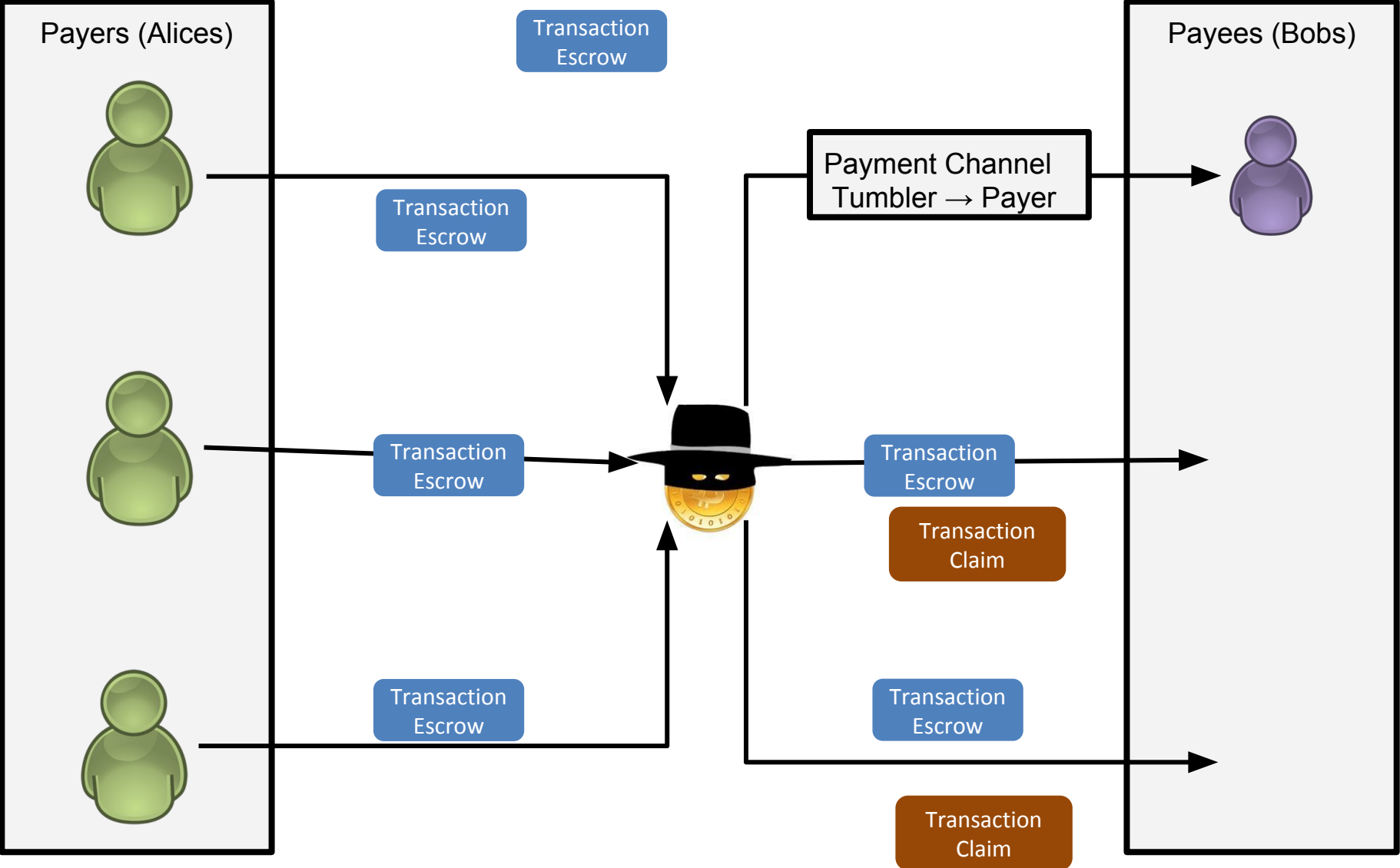
# TumbleBit: Protocol Overview



If Tumbler corrupts  $z$ ,  $c$ ,  $X$ , or  $q$  it can cheat Alice or Bob!



# Payment Hubs: Privacy

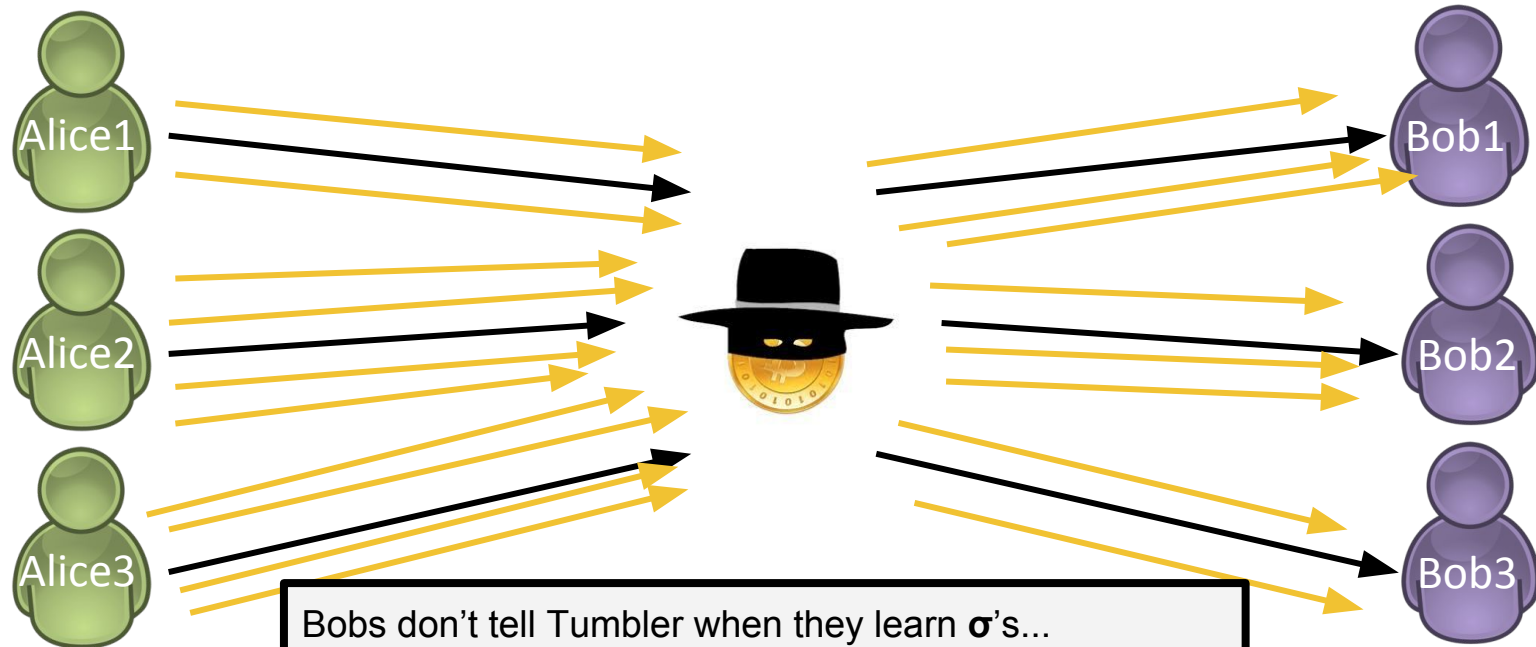


# TumbleBit: Phases and Privacy

1. **Escrow Phase:** All payment channels setup.

2. **Payments Phase (~1 month):** Alices make many payments to Bobs.

3. **Cashout Phase:** Bobs and Alices close their payment channels.



## Tumbler learns two sets of things:

1. that an Alice paid an unknown party at time  $t$ ,
2. during the payment phase the total # of payments each Bob received..

# Puzzle-Promise-Protocol

At the end of this protocol: Bob should be convinced that for a  $(z, c)$ :

1. The ciphertext  $c$  decrypts to  $\sigma$  under a key  $\epsilon$  i.e  $\text{Dec}(\epsilon, c) = \sigma$
2. **AND** the key  $\epsilon$  is the solution to the RSA-puzzle  $z$  i.e  $z = \epsilon^{pk} \text{ mod } N$

The protocol should never: allow Bob to learn a valid  $\sigma$  (without paying Tumbler).

T-PK,  
T-SK.



Tumbler

Why prevent  
 $\sigma$  allows B  
Thus, Alice

1. Bob creates and randomly permutes:  
 $m$  - valid transactions (reals) ■ ■ ■  
 $n$  - invalid transactions (fakes) ❌ ❌ ❌  
 $B = A$  randomly permuted list of the  
 real and fake transactions hashes.



Bob

**TumbleBit sets ( $m = 42, n = 42$ ):**

Prob.(Tumbler successfully cheats) =  $2^{-80}$

2. Tumbler signs each  $B_i$

For all  $B_i$  in  $B$ :  $z_i = \epsilon_i^{pk} \text{ mod } N, \sigma_i = \text{Sig}(T-SK, B_i), c_i = \text{Enc}(\epsilon_i, \sigma_i)$

$(z_1, c_1), (z_2, c_2), (z_3, c_3), (z_4, c_4), (z_5, c_5), (z_6, c_6)$

$B = \{R, F, F, R, F, R\}$

$\epsilon_2, \epsilon_3, \epsilon_5$

3. Bob reveals which  
of the  $B$ 's are fake.

4. Tumbler  
confirms fakes  
are really fakes.  
Reveals fake  $\epsilon$ 's.

5. Bob checks that  
Tumbler computed  
fakes honestly.

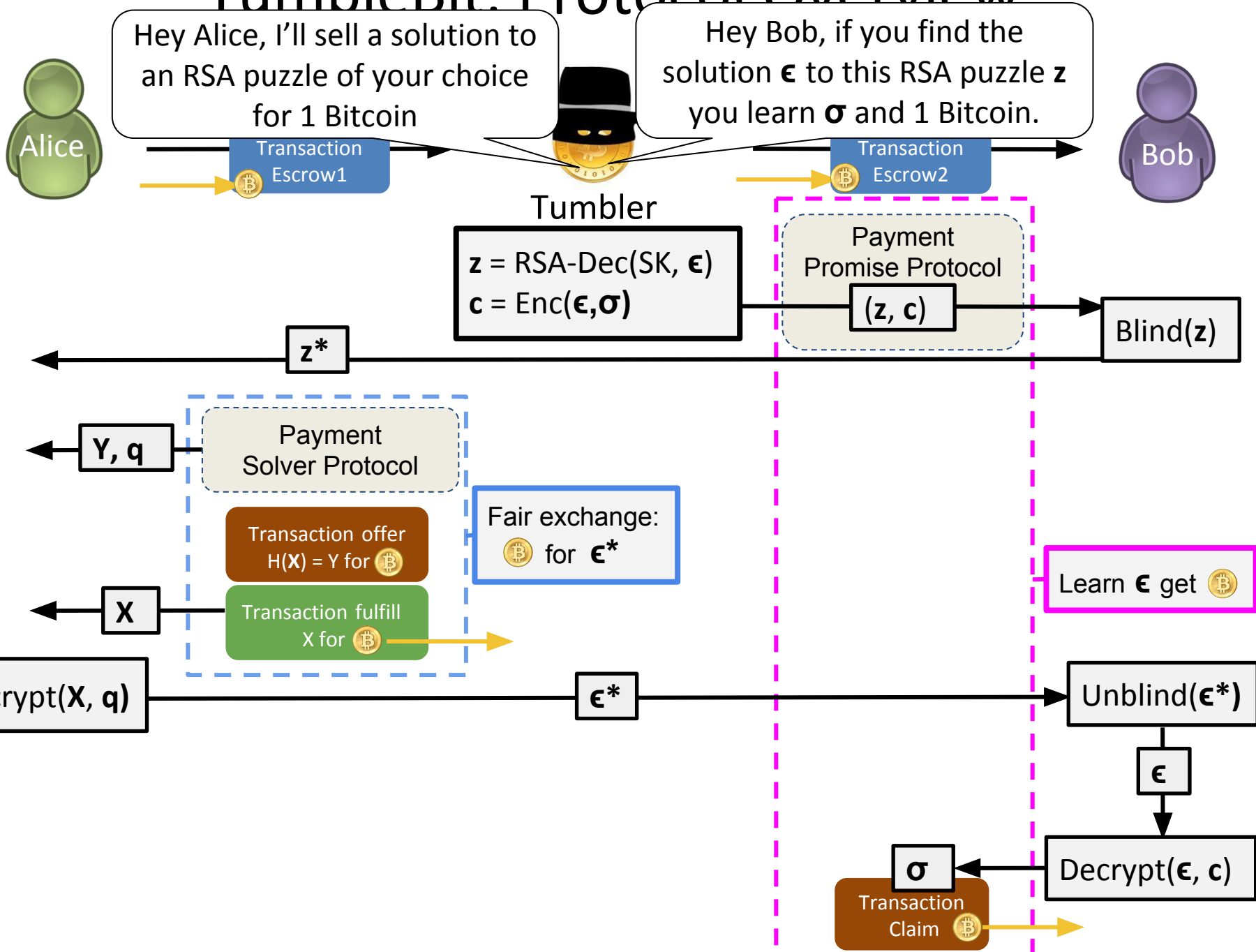
6. Bob and Tumbler run "the quotient protocol" ensuring that:  
if Bob learns  $\epsilon_1$ , Bob can use that knowledge to learn  $\epsilon_4, \epsilon_6$ .

If Tumbler computes any  $(\epsilon_i, \sigma_i)$  of the reals correctly then Bob learns a  $\sigma$ /gets paid,  
**Thus**, to cheat Bob, Tumbler must all corrupt all the reals and none of the fakes.

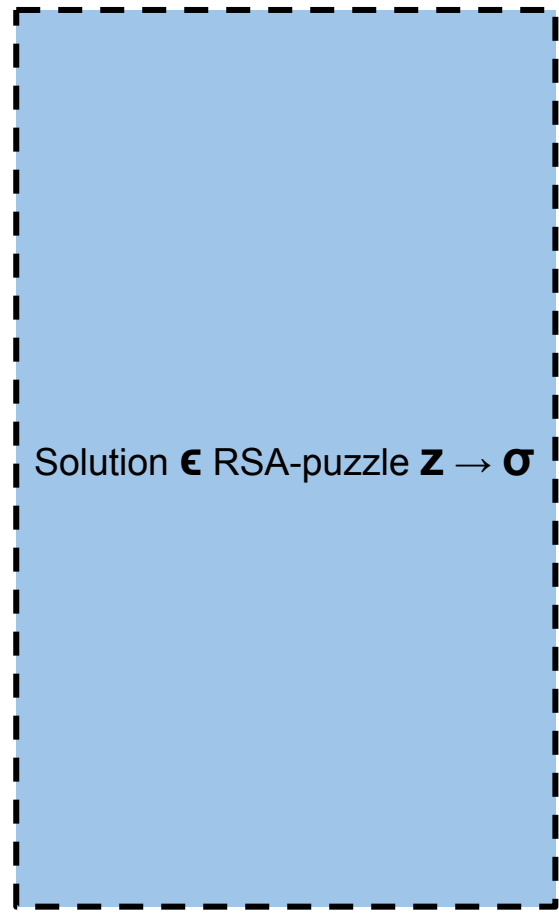
Prob(Tumbler successfully cheats) =  $1 / \binom{m+n}{m}$



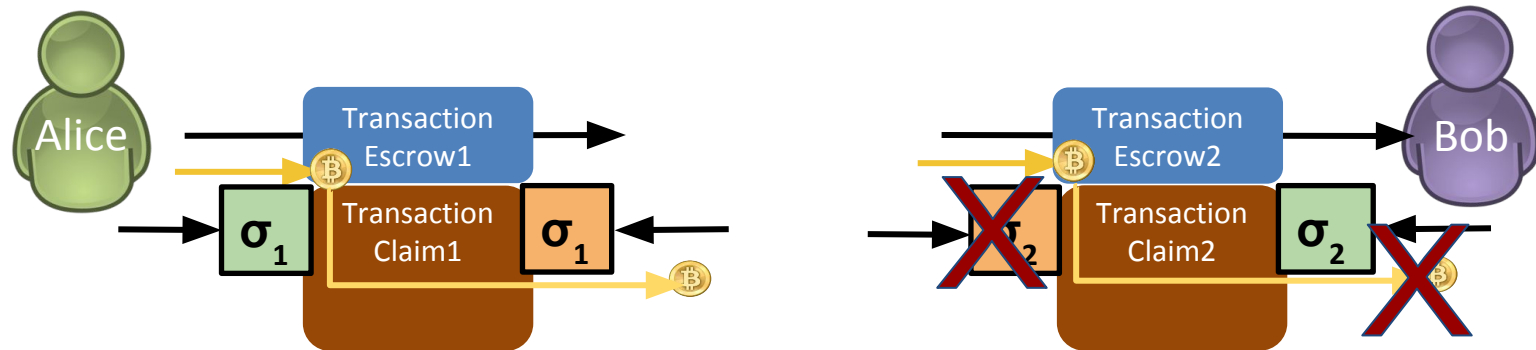
# TumbleBit: Protocol Overview



# TumbleBit: Protocol Overview



# TumbleBit Protocol



Alice signs Claim1

Payment Hub and Bob could sign and post both claim transactions, paying 1 Bitcoin from Alice to Bob via the Payment Hub.

**...But what if the hub is malicious,**

**Atomicity:** If Claim1 and Claim2 happen atomically then theft is prevented.

Hash locks provide this property.

Puzzle-Solver-Protocol:

Tumbler convinces Alice the preimage  $X$  where  $\text{Hash}(X) = Y$  will allow her to learn  $\epsilon^*$ .

Puzzle-Promise-Protocol:

Tumbler convinces Bob that the solution to RSA puzzle  $Z$  is a value  $\epsilon$  which allows him learn  $\sigma$  and he can claim 1 Bitcoin.

**But what if the Tumbler is malicious and cheats Alice and Bob?**



Tumbler



Bob

$$z = \epsilon^{pk} \text{ mod } N$$
$$c = \text{Enc}(\epsilon, \sigma)$$

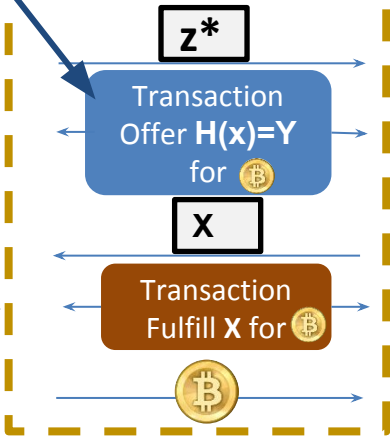
$(z, c)$

Transaction Offer  $\text{Bitcoin}$  for  $\sigma$

Sig Condition:  $\sigma$  such that  $\sigma$  is a valid signature.

Hash Condition:  $X$  such that  $\text{Hash}(X) = Y$ .

$z^*$



Fair exchange 1:  
B: Gives  $\sigma$   
T: Gives 1 bitcoin

Fair exchange 2:  
A: Gives 1 bitcoin  
T: Gives 1  $\epsilon^*$

$\epsilon^*$

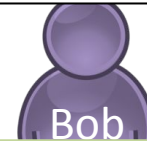
$\sigma$

Transaction Fulfill  $\text{Bitcoin}$  for  $\sigma$

# Alice pays Bob with RSA Puzzles

Hey Alice, I'll sell a solution to an RSA puzzle of your choice for 1 Bitcoin

Hey Bob, if you find the solution  $\epsilon$  to this RSA puzzle  $z$  you get 1 Bitcoin.



Remember how Payment Channels work:



Transaction Escrow

Transaction Claim1



$\sigma$

+1 BTC

$\epsilon$

Tumbler can encrypt  $\sigma$  under an RSA-puzzle

$$z = \epsilon^{pk} \text{ mod } N$$
$$c = \text{Enc}(\epsilon, \sigma)$$

$(c, z)$

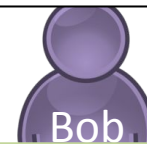
If Bob learns the solution  $\epsilon$  to  $z$   
Bob can decrypt  $c$  to  $\sigma$  and get 1 BTC.

+1 BTC

# Alice pays Bob with RSA Puzzles

Hey Alice, I'll sell a solution to an RSA puzzle of your choice for 1 Bitcoin

Hey Bob, if you find the solution  $\epsilon$  to this RSA puzzle  $z$  you get 1 Bitcoin.



Remember how Payment Channels work:



Transaction Escrow

Transaction Claim1



$\sigma$

+1 BTC

$\epsilon$

Tumbler can encrypt  $\sigma$  under an RSA-puzzle

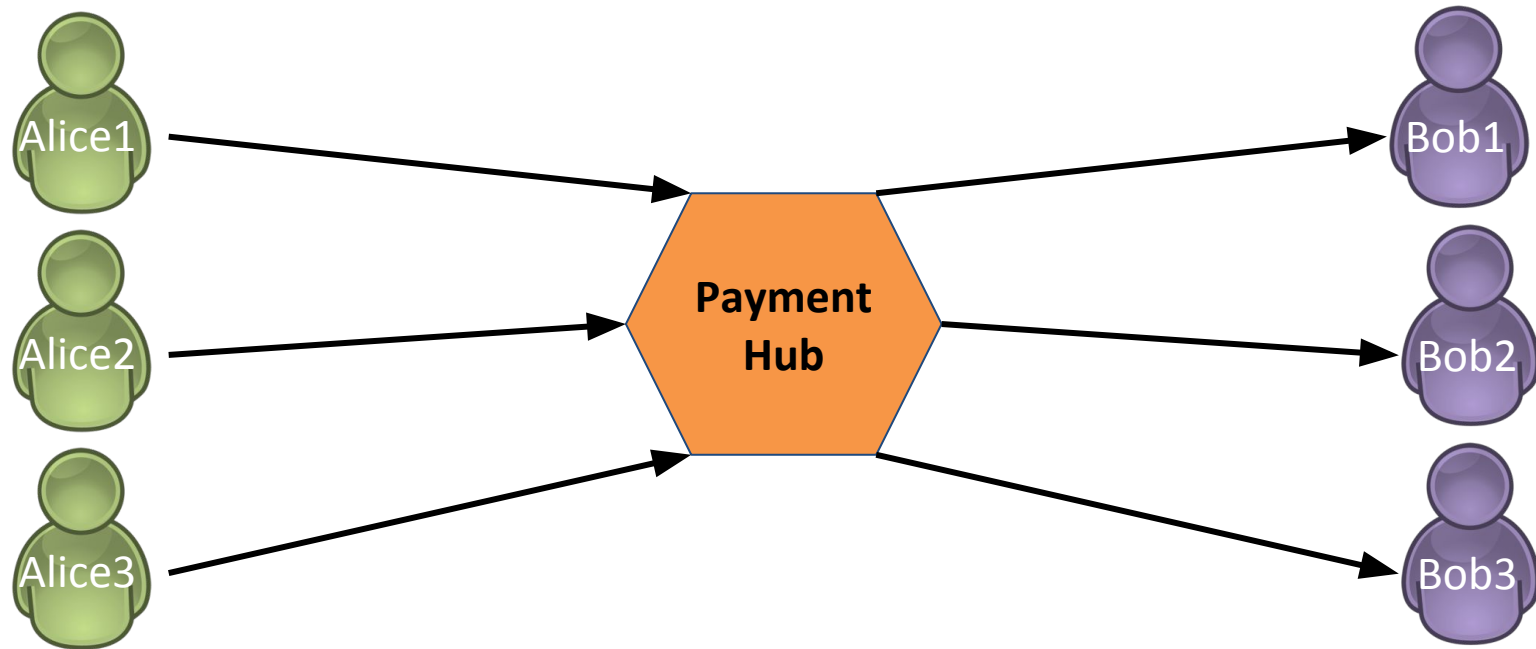
$$z = \epsilon^{pk} \text{ mod } N$$
$$c = \text{Enc}(\epsilon, \sigma)$$

$(c, z)$

If Bob learns the solution  $\epsilon$  to  $z$   
Bob can decrypt  $c$  to  $\sigma$  and get 1 BTC.

+1 BTC

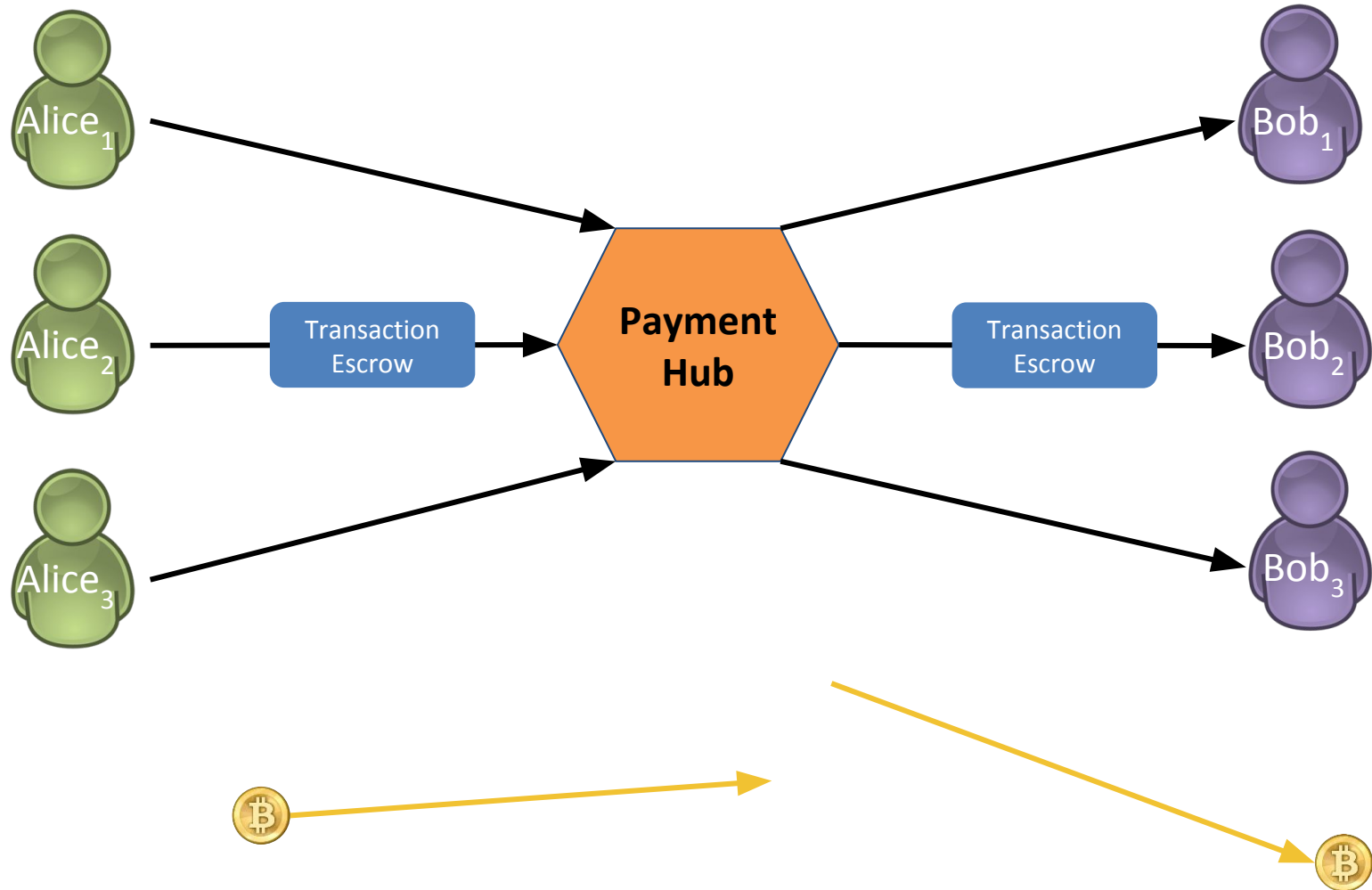
# Payment Hub: Privacy



TumbleBit improves payment hubs so that for each payment the payer can not be linked to the payees.

# Payment Hub

A payment hub: routes payment channels

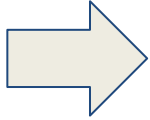




# Introduction



# Outline



- Payment hubs
  - Bitcoin transactions/payment channels
  - What are Bitcoin payment hubs?
  - Scalability benefits of payment hubs
  - Are payment hubs private?
- TumbleBit as a Payment Hub
  - RSA-blind puzzles
  - TumbleBit as an unlinkable payment hub
  - Ensuring fair-exchange (TumbleBit can't steal)
  - Puzzle-Promise-Protocol

# Motivation

## Technical challenges facing Bitcoin: Privacy, Scalability

### Privacy:

- Bitcoin is not anonymous
- Payment history is saved to the blockchain i.e. an eternal public record

### Scaling Transaction velocity:

- Transactions are confirmed on the blockchain (avg wait time ~10 mins)
- No confirmation = double spending possible

### Scaling Transaction volume:

- Bitcoin: 7 transactions/sec max throughput[1]
- Visa (average): 2000 transactions/sec[1]
- Visa (peak): 56,000 transactions/sec[1]
- Limiting factor is space in Bitcoin's blockchain

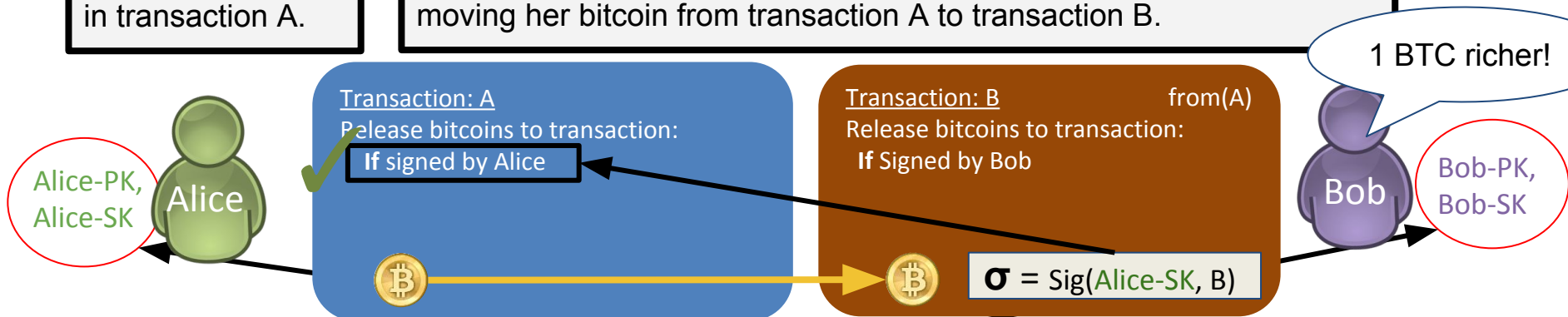
TumbleBit is designed to address these challenges by providing privacy and scalability **without** introducing trust.

[1]: 'On Scaling Decentralized Blockchains (A Position Paper)' Croman, et al.

# Bitcoin Transactions

1. Alice has 1 BTC in transaction A.

2. To setup a payment of 1 BTC to Bob, Alice creates a transaction B moving her bitcoin from transaction A to transaction B.

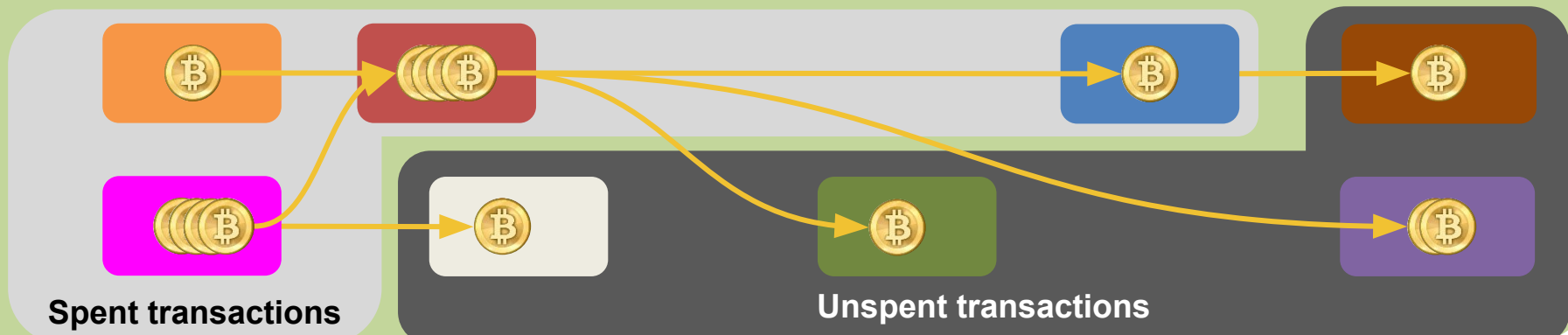


Transaction conditions ("release bitcoins to transaction if") are programmable:

- via a very limited non-turing complete language called *Script*,
- can verify multiple signatures and perform a few other operations.

I will talk more about it later.

Payment in Bitcoin occurs by transferring bitcoins in one transaction to a new transaction...  
...thus, ownership is merely holding a secret which can authorize such transfers.



# Unidirectional Payment Channels

1. Alice opens a payment channel by placing 4 BTC in an escrow transaction.

2. Escrow transaction confirmed on the blockchain.

Alice-PK,  
Alice-SK



Transaction: Escrow  
Release bitcoins to transaction:  
If signed by Alice & Bob  
or  
If signed by Alice & 1 month has passed



3. Alice can pay Bob multiple times by signing Claim transactions.

Transaction: Claim1  
3 Bitcoins to Alice, 1 Bitcoin to Bob

Sig(Alice-SK, Claim1)

Transaction: Claim2  
2 Bitcoins to Alice, 2 Bitcoin to Bob

Sig(Alice-SK, Claim2)

Transaction: Claim3  
1 Bitcoins to Alice, 3 Bitcoin to Bob

Sig(Alice-SK, Claim3)

Sig(Bob-SK, Claim3)

Transaction: Claim4  
0 Bitcoins to Alice, 4 Bitcoin to Bob



Bob-PK,  
Bob-SK

Bob has 0 BTC
Bob has 1 BTC
Bob has 2 BTC
Bob has 3 BTC in the channel.

3 BTC to Bob



1 BTC to Alice



4. Bob closes the channel by signing Claim3 and posting the transaction to the blockchain.

## Advantages of Payment channels

**Scales Tx volume:** Two transaction on the blockchain allow Alice to pay Bob many times.

**Scales Tx velocity:** Risk of Double spending  $\sim=0$  so payments happen in milliseconds.

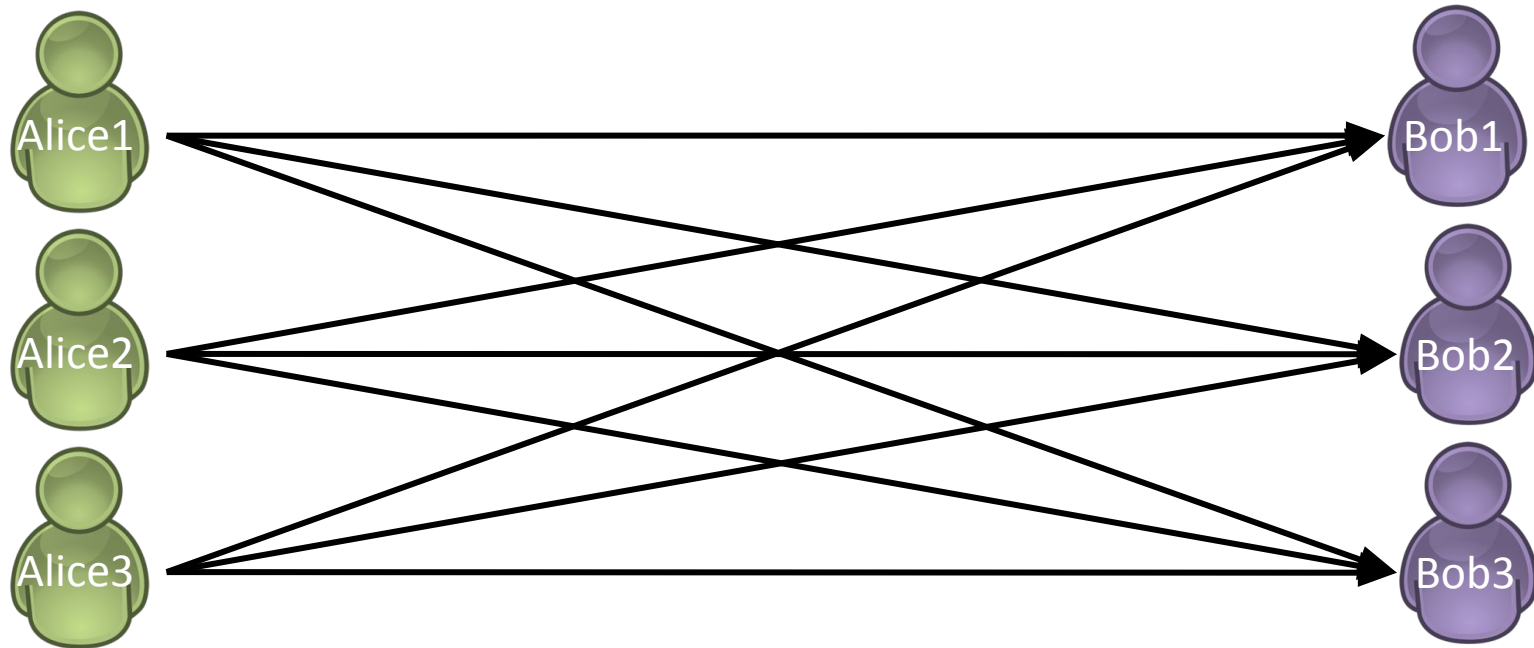
**No trust required:** Neither Alice nor Bob can cheat each other.

If Bob walks away Alice gets her money back after 1 month.

# Unidirectional Payment Channels

## Disadvantages of Payment channels:

1. To pay many different Bobs, requires many different channels.
2. Each channel setup is expensive in time (~10 minutes)
3. **...and** money (i.e. BTC sitting in escrows that can't be used).

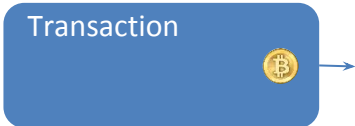
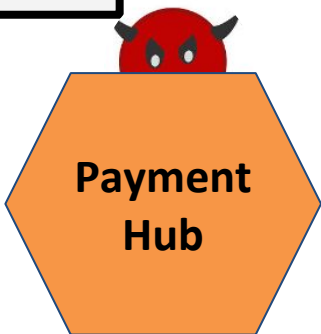


A Payment Hub solves these disadvantages.

# Payment Hub: Details

**But what if the payment hub is malicious and cheats Alice and Bob?**

Alice wants to pay Bob via the payment hub.



1. Alice signs a transaction paying 1 BTC to the payment hub.

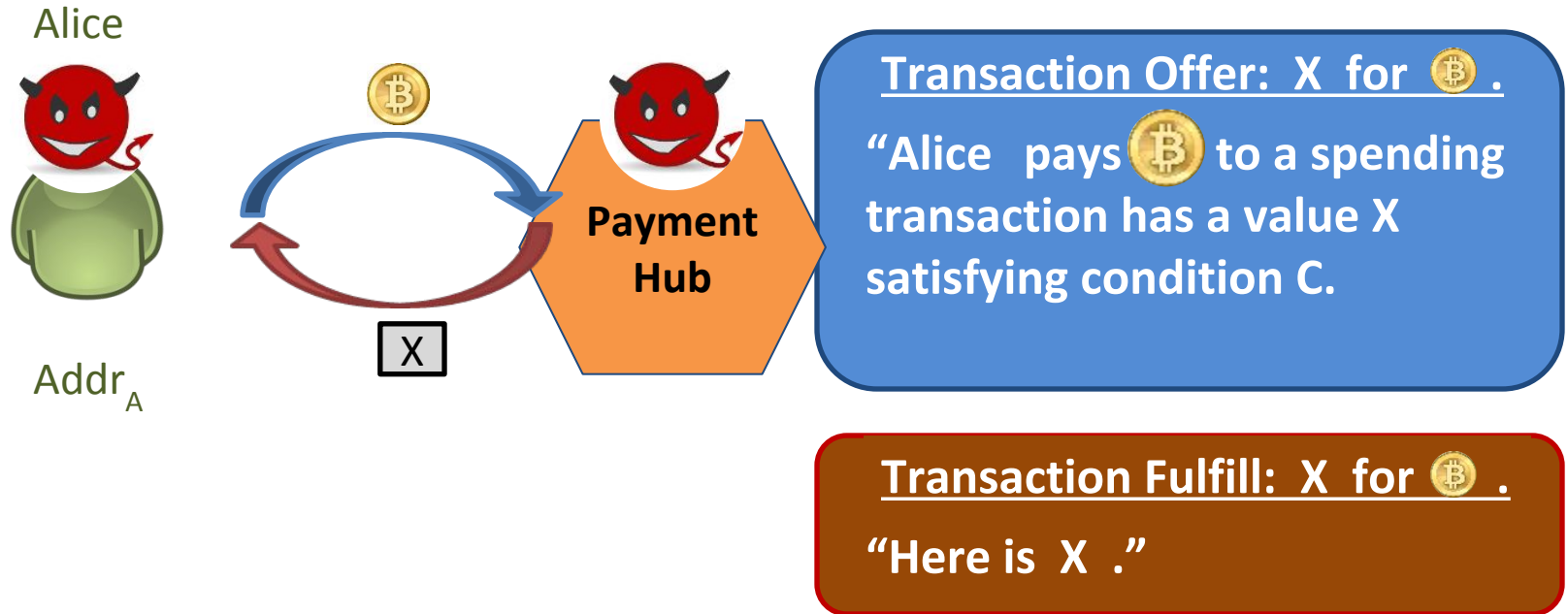
**It takes Alice's bitcoin but doesn't pay Bob.**



2. Payment hub signs a transaction paying 1 BTC to Bob.

# Bitcoin Transaction Contracts

Goal: **Fair Exchange/Atomic swaps:**

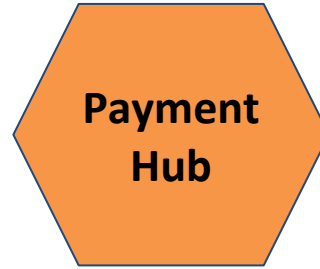


Bitcoin can only check two cryptographic conditions:

1.  $\text{Hash}(X) = Y$ ,
2. Verify ECDSA Signature on a transaction.

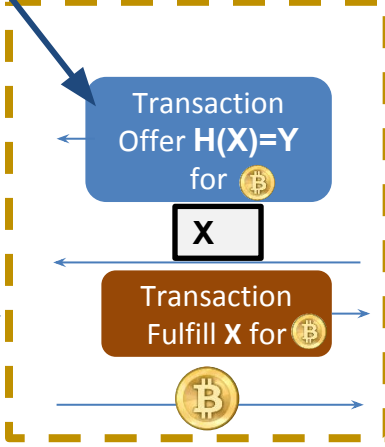


# Payment Hub: Fair Exchange



Hash Condition:  
X such that  
 $\text{Hash}(X) = Y$ .

Hash Condition:  
X such that  
 $\text{Hash}(X) = Y$ .



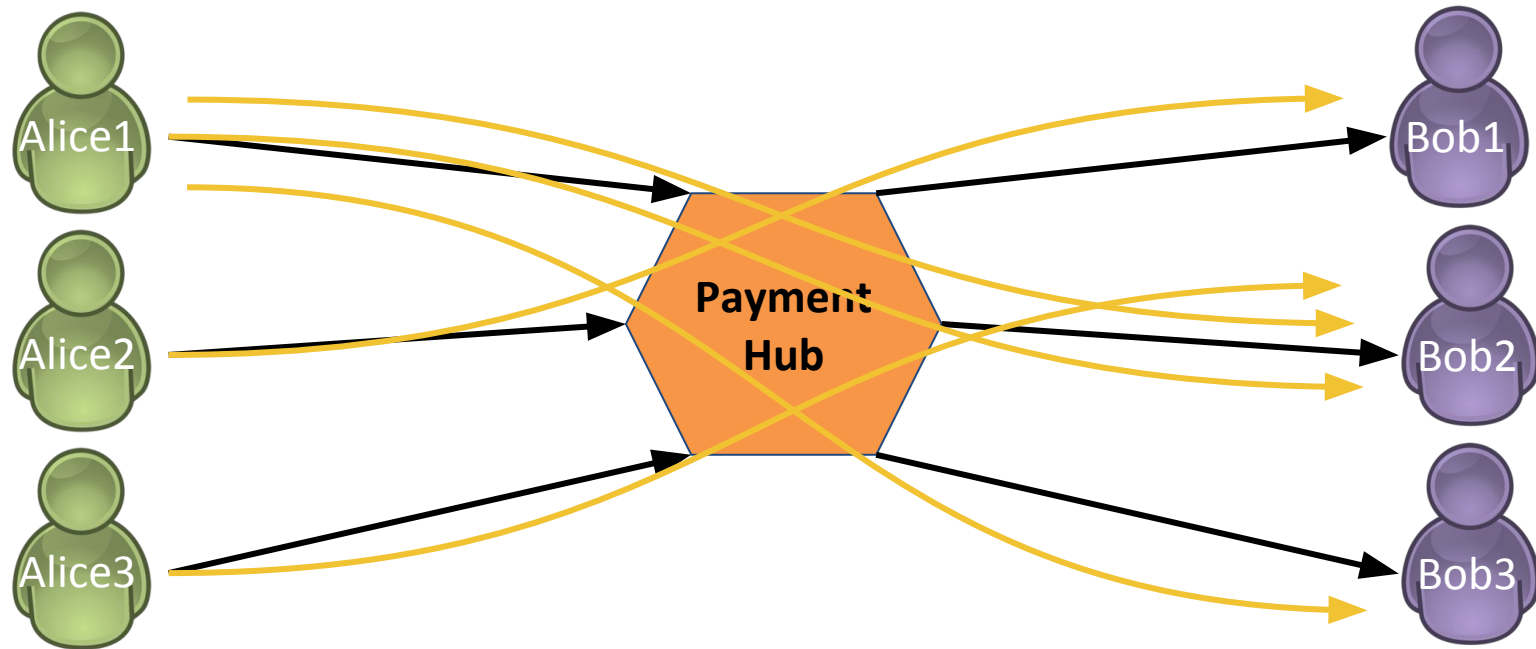
Fair exchange 1:  
H: Gives X  
B: Gets 1 bitcoin

Fair exchange 2:  
A: Gives 1 bitcoin  
H: Get X

Fair exchange prevents the Payment Hub from stealing.

# Payment Hub: Privacy

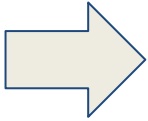
While payment hubs are convenient, they do not offer any privacy against the payment hub. The payment hub can trivially link the payer to the payee via the  $H(X)=Y$  used to ensure atomicity.



TumbleBit improves payment hubs so that for each payment the payer can not be linked to the payees.

# Outline

- Payment hubs
  - Bitcoin transactions/payment channels
  - What are Bitcoin payment hubs?
  - Scalability benefits of payment hubs
  - Are payment hubs private?
- TumbleBit as a Payment Hub
  - RSA-blind puzzles
  - TumbleBit as an unlinkable payment hub
  - Ensuring fair-exchange (TumbleBit can't steal)
  - Puzzle-Promise-Protocol



# RSA Puzzles

- An RSA Puzzle is just an RSA encryption of some value  $\epsilon$ :  
$$z = \text{encRSA}(\epsilon, pk) = \epsilon^{pk} \bmod N$$
- Only the party that knows  $sk$  can solve RSA puzzles:  
$$\epsilon = \text{decRSA}(z, sk) = z^{sk} \bmod N = (\epsilon^{pk})^{sk} \bmod N$$

## RSA blinding can be used to blind RSA puzzles

1. Tumbler issues two puzzles.



Tumbler

$z_1$

$z_2$



$z^* = \text{Blind}(z_2)$

$\epsilon^*$

2. Bob2 blinds his puzzle and requests a solution.

$\epsilon_2 = \text{Unblind}(\epsilon^*)$

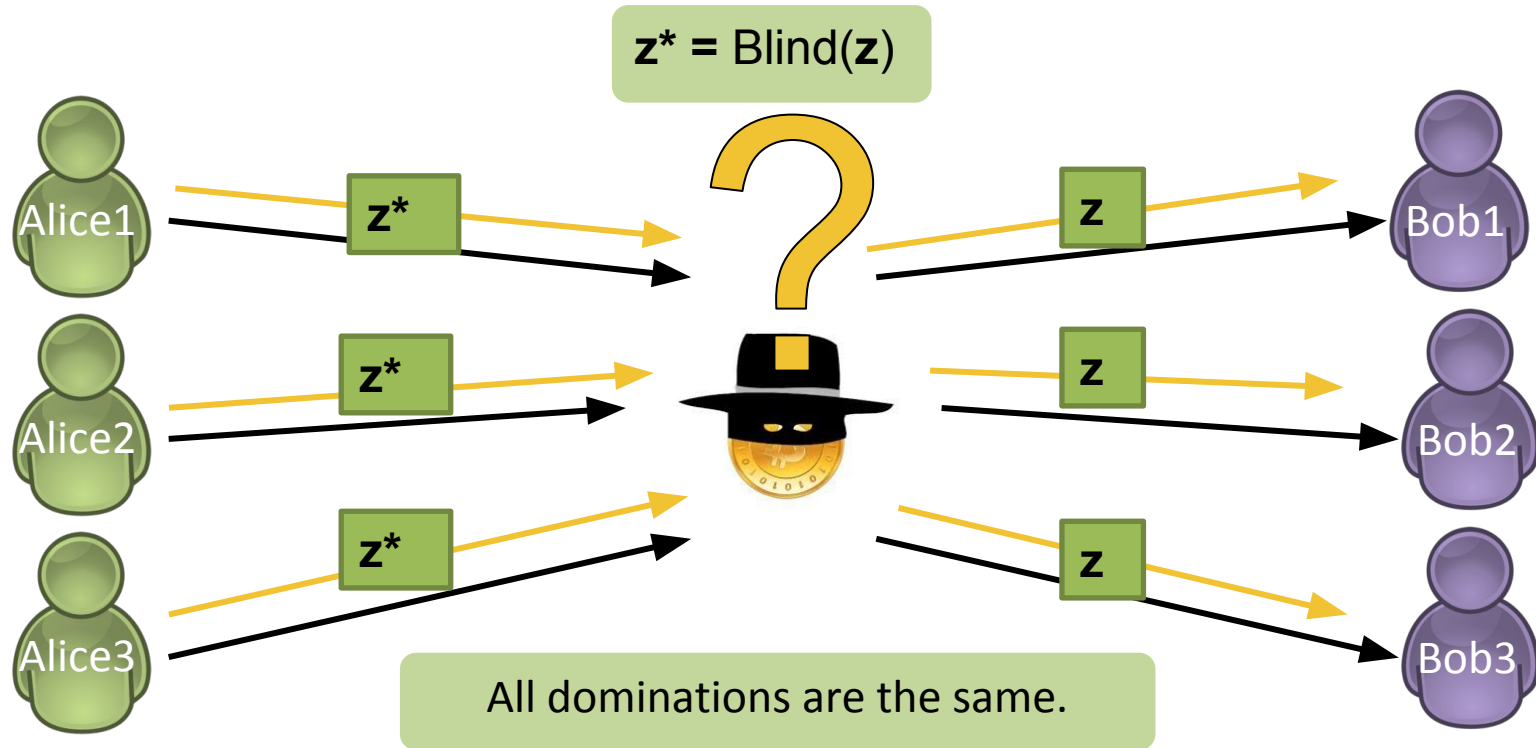
3. Tumbler solves the blinded puzzle and generates a blinded solution  $\epsilon^*$ .

4. Bob2 finds the solution to  $z_2$  by unblinding  $\epsilon^*$ .

Tumbler can not link the blinded RSA puzzle it solves to any of the RSA puzzles it issues.

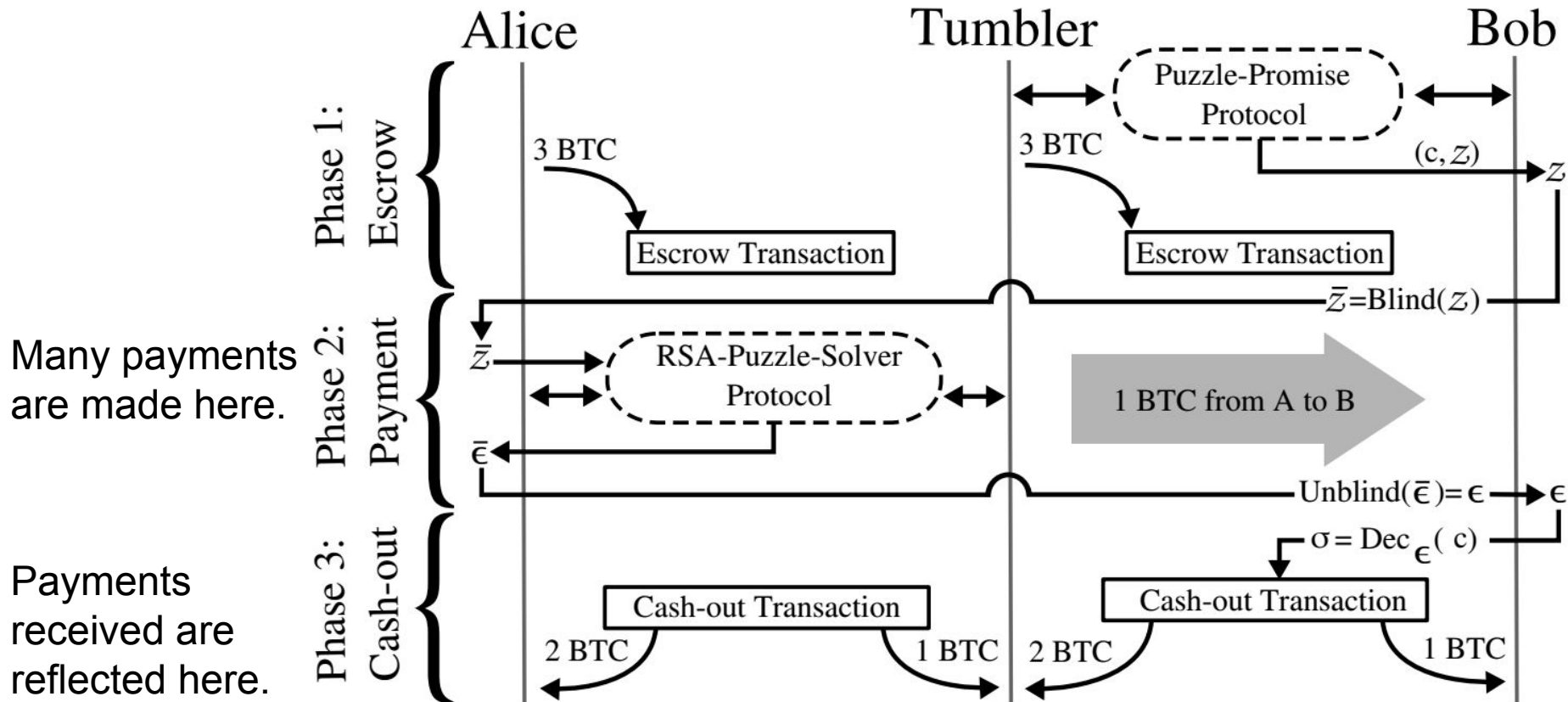
# Unlinkable Payments

We can use RSA puzzles to hide the link between payers and payees.



...but how do we ensure that the tumbler does not cheat.

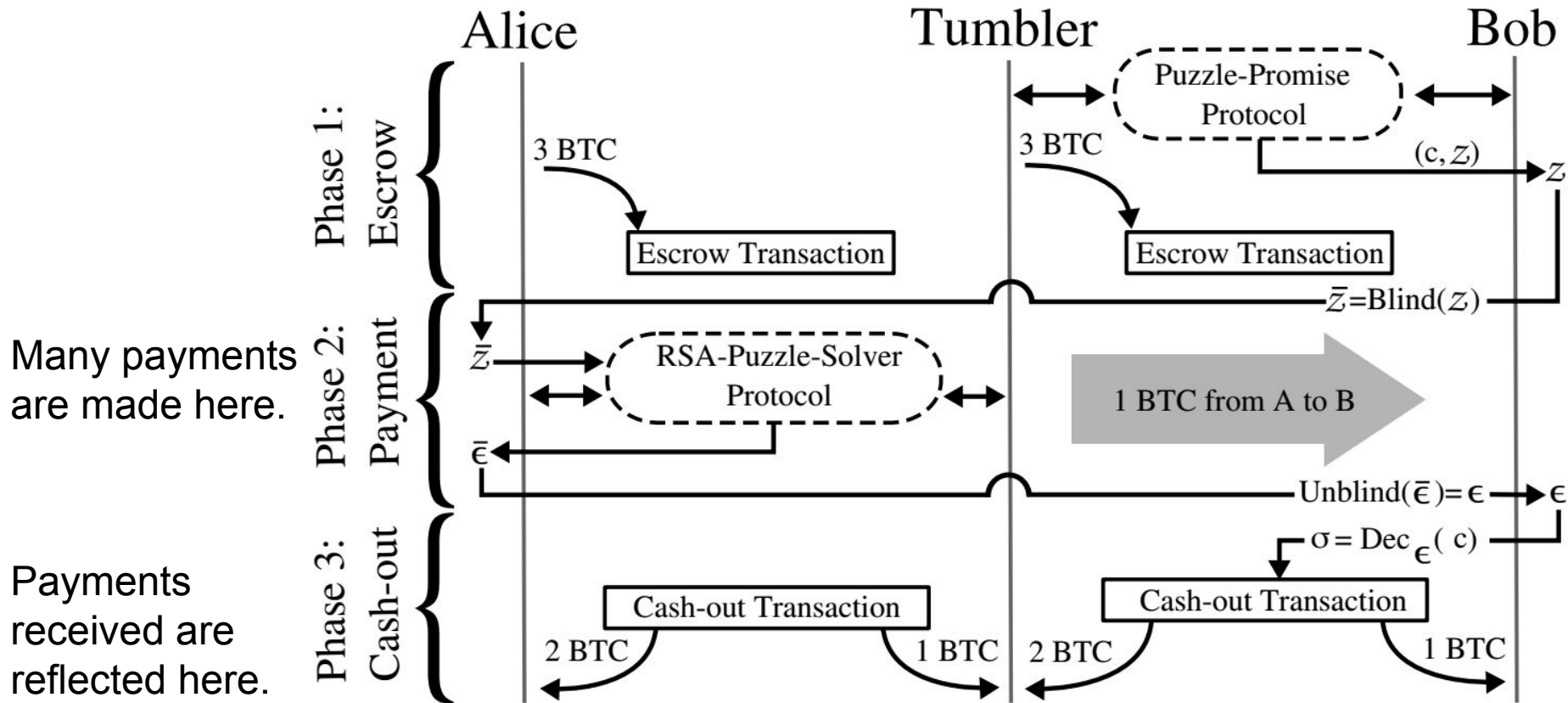
# Puzzle-Promise-Protocol



## Payment unlinkability:

1. In payment: Tumbler can see that Alice paid (but not who she paid)
2. In cashout: Tumbler learns aggregate funds received by Bob.

# Unlinkability

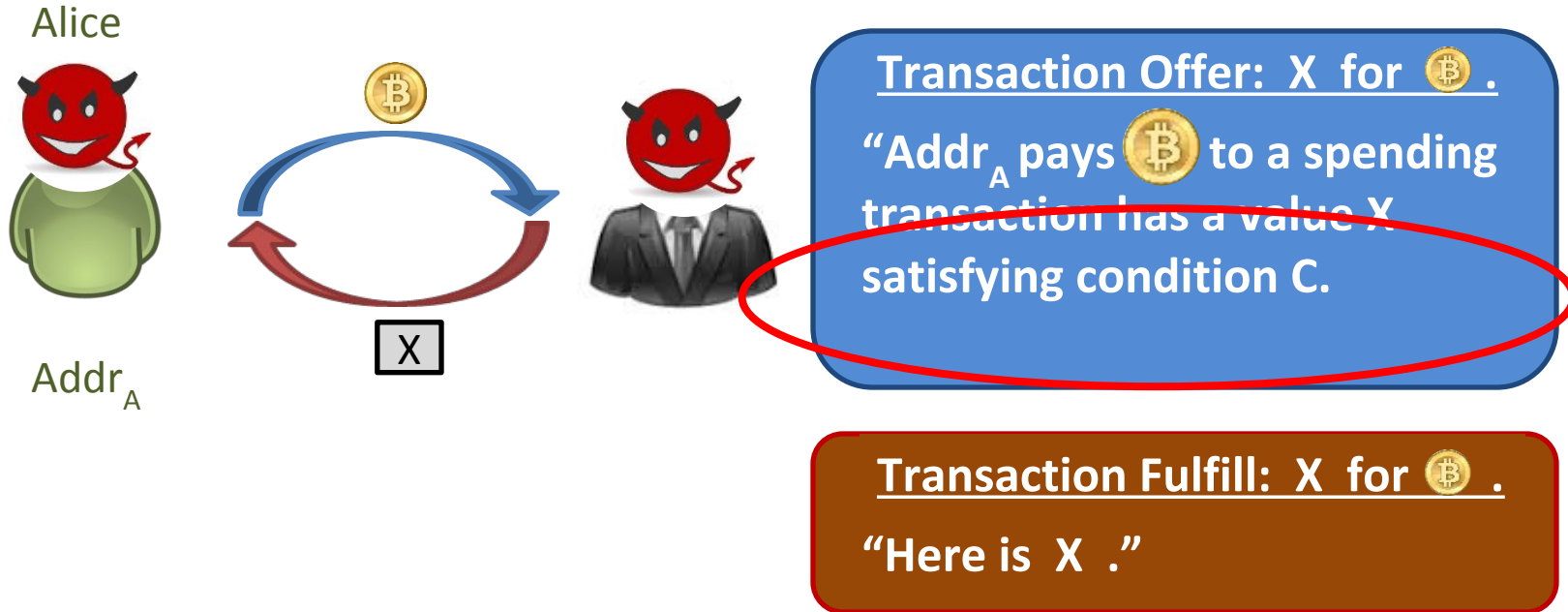


## Payment unlinkability:

1. In payment: Tumbler can see that Alice paid (but not who she paid)
2. In cashout: Tumbler learns aggregate funds received by Bob.

# Bitcoin Transaction Contracts

Goal: **Fair Exchange/Atomic swaps:**



Bitcoin transaction scripts are very limited.

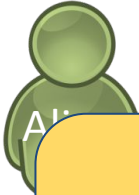
We can only check two types of cryptographic conditions C:

1.  $\text{Hash}(X) = Y$ ,
2.  $\text{ECDSA\_CheckSignature}(\text{Tx}, \text{PUBLIC\_KEY}) = \text{TRUE}$



# TumbleBit: Paying with RSA-Puzzles

But what if the Tumbler is malicious and cheats Alice and Bob?



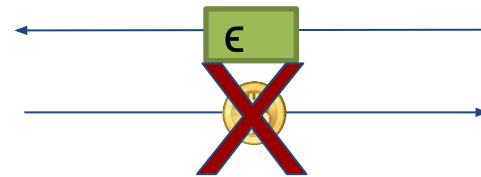
To prevent cheating we develop protocols that ensure blockchain mediated fair exchange.

blinds  
e.

Alice buys a solution.



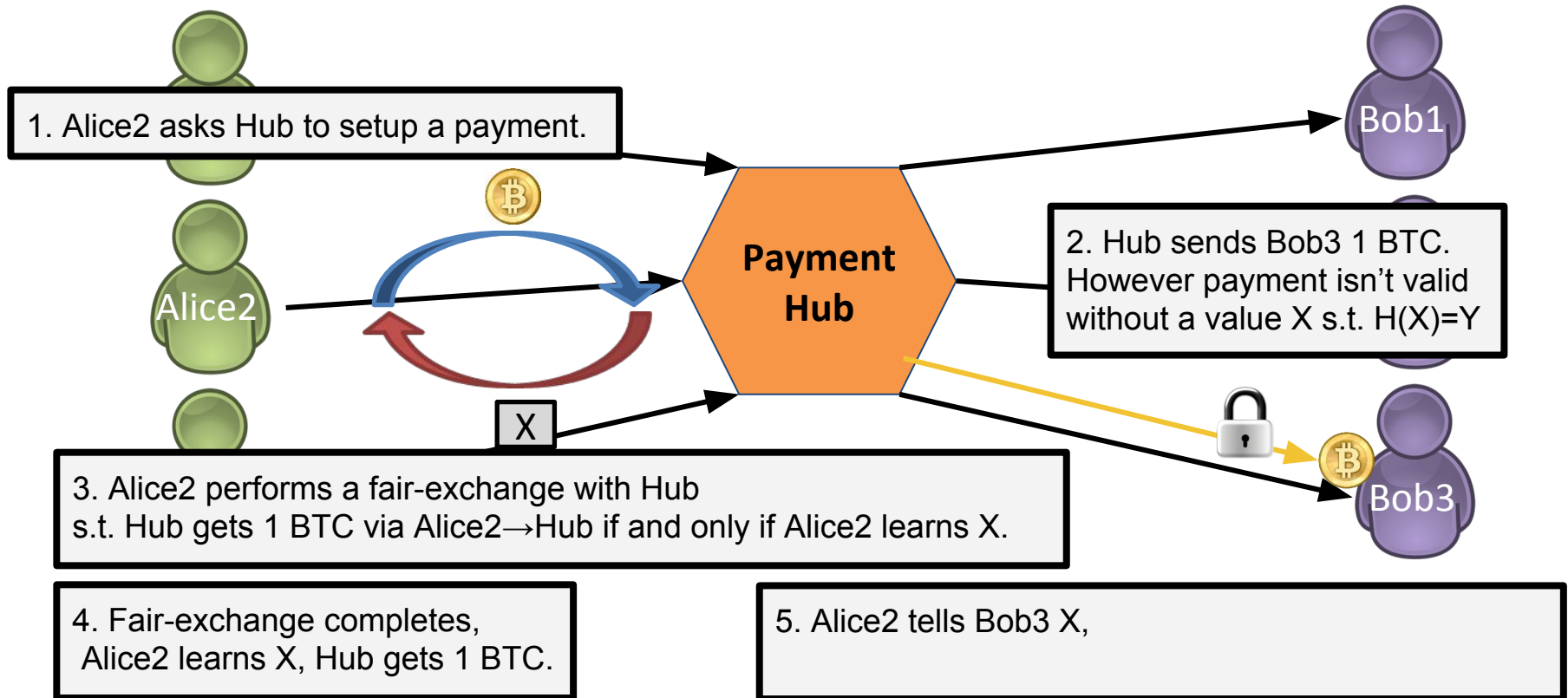
Tumbler could take Alice's money and fail to provide a solution?



Bob unblinds Puzzle.

Tumbler could refuse to pay for a solution?

# Payment Hubs: Preventing Theft

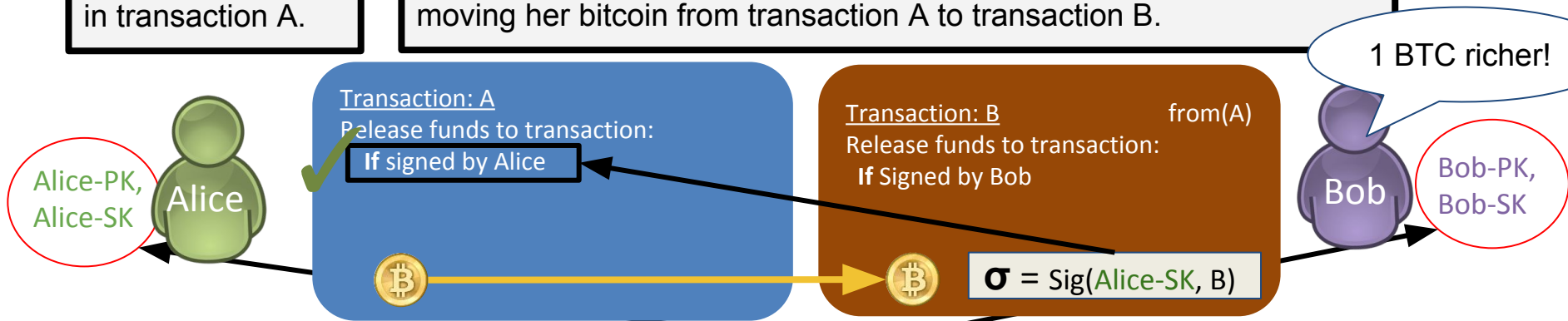


We want to ensure that the transaction Alice2→Hub is atomic with Hub→Bob3.

# Background: Bitcoin Transactions

1. Alice has 1 BTC in transaction A.

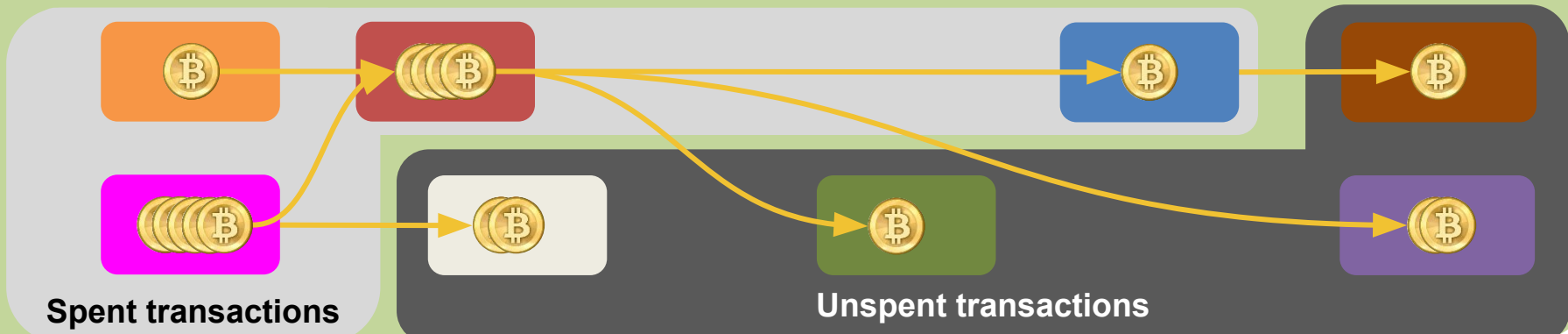
2. To setup a payment to Bob of 1 BTC Alice creates a transaction B moving her bitcoin from transaction A to transaction B.



3. Alice then signs transaction B to fulfill A's condition...

...thus transferring that bitcoin from transaction A to transaction B.

Payment in Bitcoin occurs by transferring bitcoins in one transaction to a new transaction...  
...thus, ownership is merely holding a secret key which can authorize such transfers.



# Background: Payment Hub

1. Alice opens a payment channel by placing 4 BTC in an escrow transaction.

2. Escrow transaction confirmed on the blockchain.

Alice-PK,  
Alice-SK



Transaction: Escrow  
Release funds to transaction:  
If signed by A & B  
or  
If signed by A & 4 days have passed.



2. Alice can pay Bob multiple times by signing Claim transactions.

Transaction: Claim1 from(Escrow)  
3 Bitcoins to Alice, 1 Bitcoin to Bob

Sig(Alice-SK, Claim1)

Transaction: Claim2 from(Escrow)  
2 Bitcoins to Alice, 2 Bitcoin to Bob

Sig(Alice-SK, Claim2)

Transaction: Claim3 from(Escrow)  
1 Bitcoins to Alice, 3 Bitcoin to Bob

Sig(Alice-SK, Claim3)

Sig(Bob-SK, Claim3)

Transaction: Claim4 from(Escrow)  
0 Bitcoins to Alice, 4 Bitcoin to Bob



Bob-PK,  
Bob-SK

Bob has 0 BTC
Bob has 1 BTC
Bob has 2 BTC
Bob has 3 BTC in the channel.

1 BTC to Alice



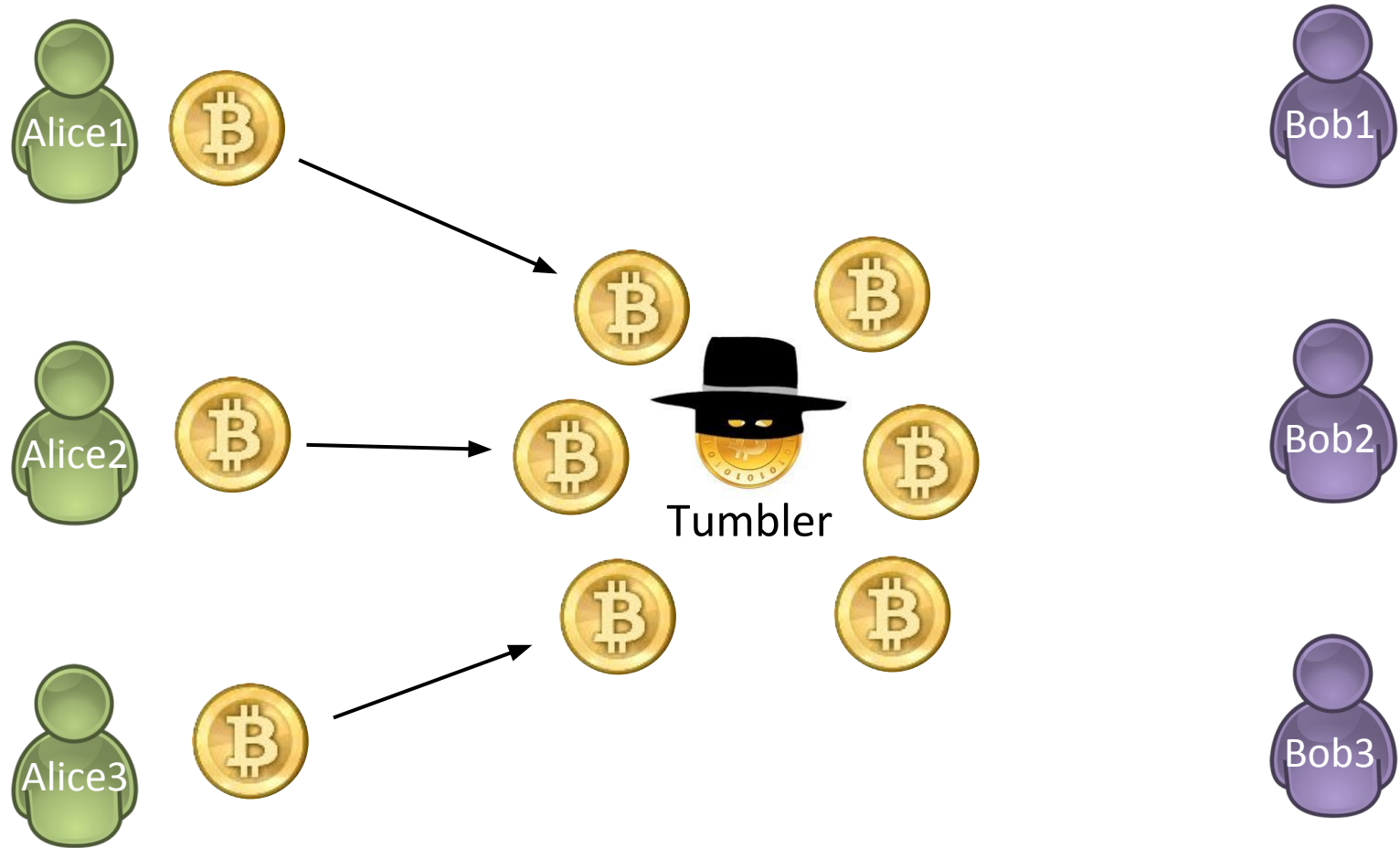
3. Bob closes the channel by signing Claim3 and posting the transaction to the blockchain.

3 BTC to Bob



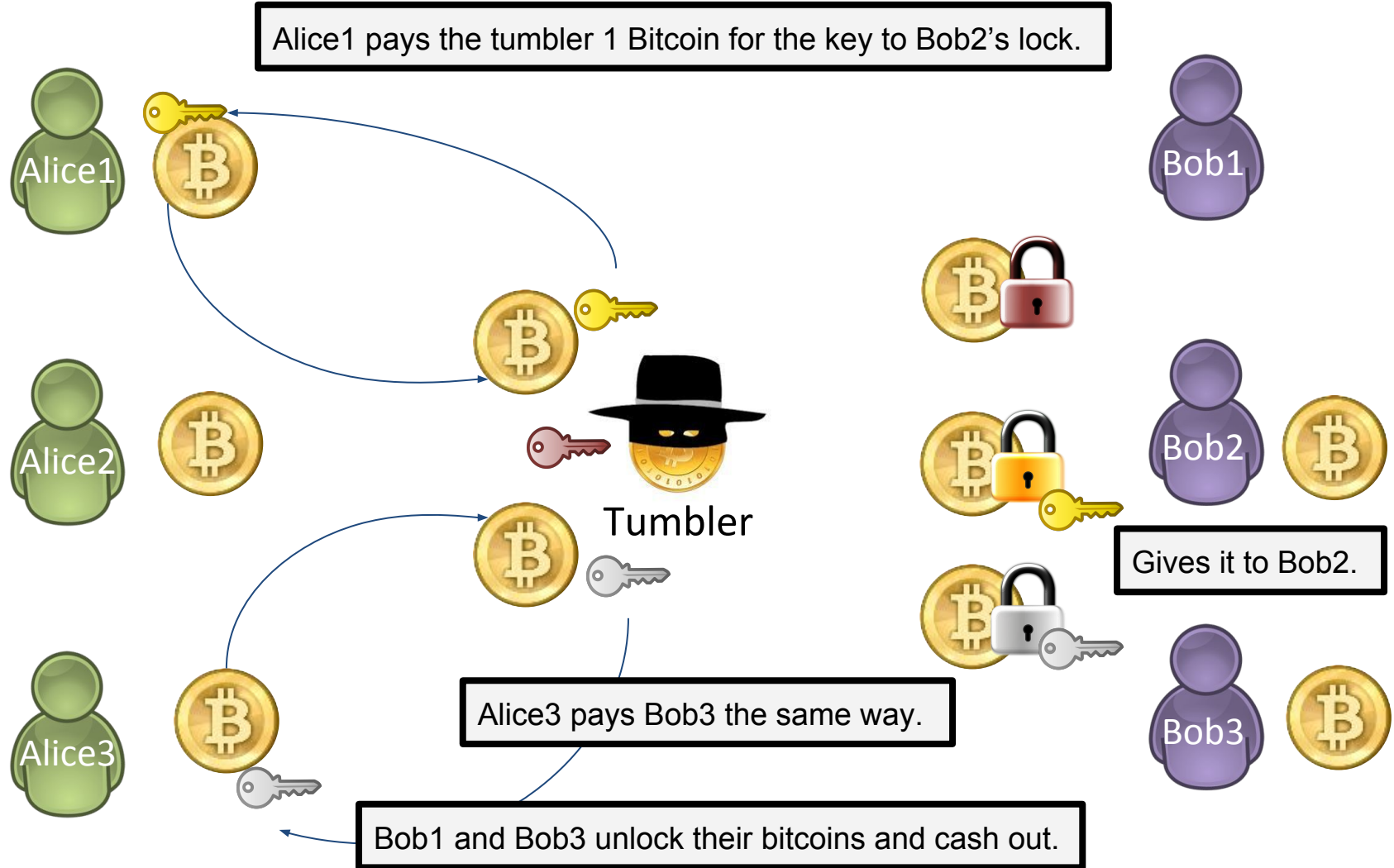
Alice was able to make N instant transactions to Bob.

# TumbleBit: The Basic Idea



Intuition: Tumbler gives out locked bitcoins and sells keys.

# TumbleBit: Overview



Intuition: Tumbler gives out locked bitcoins and sells keys.

# Related Work

## New Cryptocurrencies

Not compatible with bitcoin



## Bitcoin-Compatible Schemes

(aka "Mixing Services")

Vulnerable to bitcoin theft



MIXCOIN  
True Anonymous Cryptocurrency

Blindcoin:



Vulnerable to DoS & Sybil Attacks



Limited Anonymity

CoinShuffle



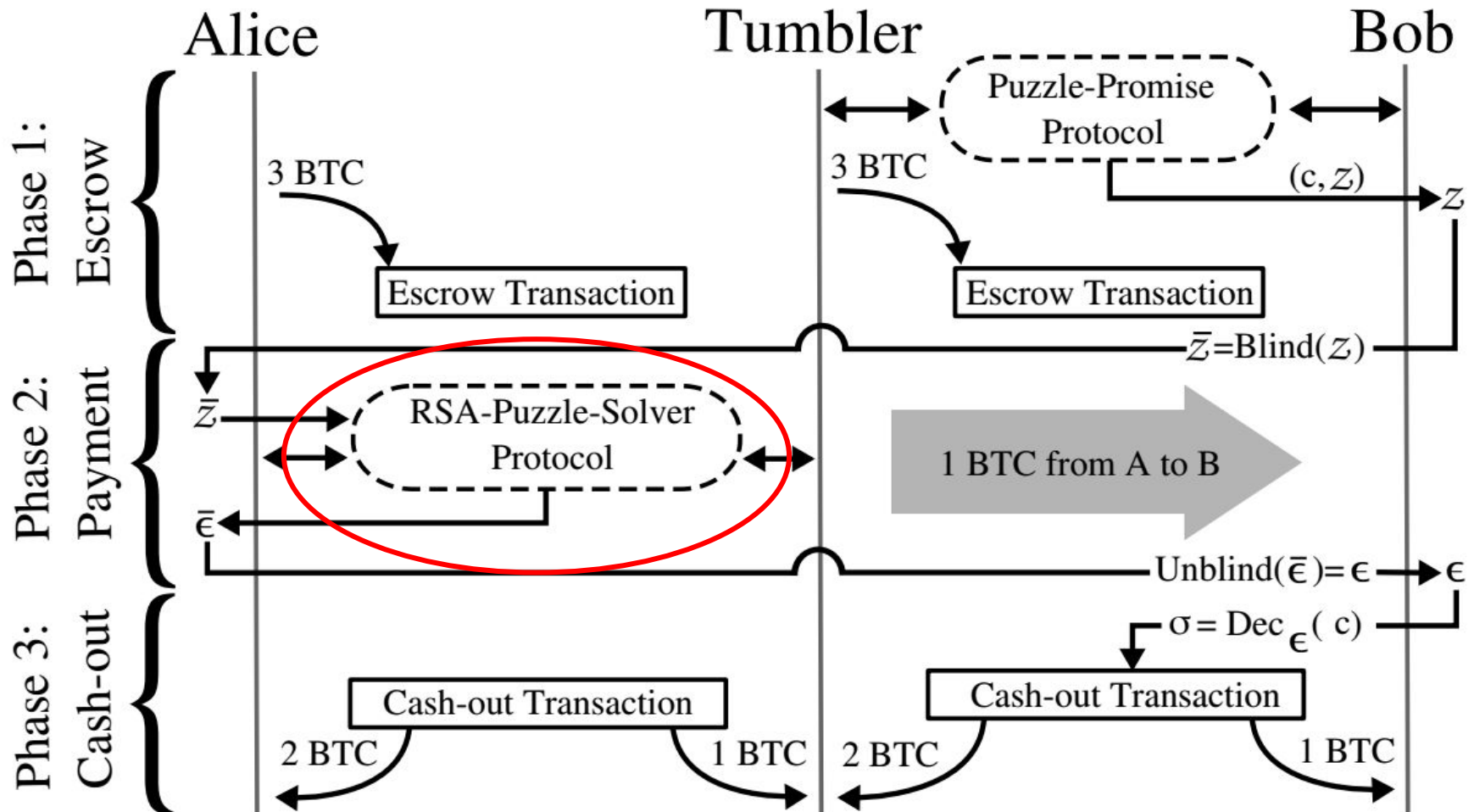
Intermediary  
breaks  
anonymity

Mixing takes  
hours

Xim

TumbleBit

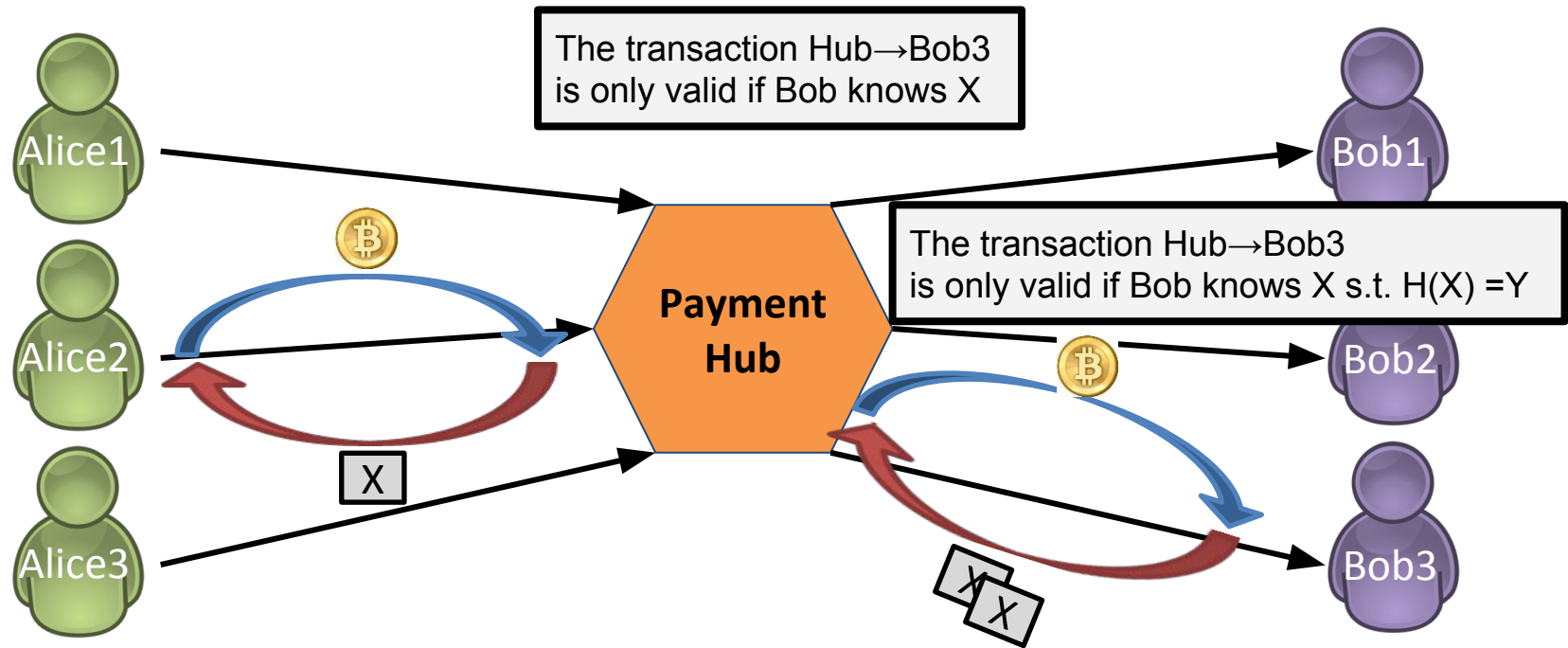
# RSA-Puzzle-Solver Protocol



I'm only going to walk through the RSA-Puzzle-Solver Protocol, but it is similar to the Puzzle-Promise-Protocol.



# Payment Hubs: Preventing Theft



We want to ensure that the transaction Alice2→Hub is atomic with Hub→Bob3.

# Puzzle-Solver-Protocol

Alice $\mathcal{A}$	Tumbler $\mathcal{T}$
Input: Puzzle $y$	Secret input: $sk$

Blinded puzzle

$$\boxed{z^*} = y$$

1. Prepare Real Puzzles  $R$   
 For  $i \in [m]$ , pick  $r_i \in \mathbb{Z}_N^*$   
 $d_i \leftarrow y \cdot (r_i)^{pk} \pmod N$

2. Prepare Fake Values  $F$   
 For  $i \in [n]$ , pick  $\rho_i \in \mathbb{Z}_N^*$   
 $\delta_i \leftarrow (\rho_i)^{pk} \pmod N$

3. Mix Sets.  
 Randomly permute  
 $\{d_1, \dots, d_m, \delta_1, \dots, \delta_n\}$

4. Evaluation  
 For  $i = 1, \dots, m+n$

Alice mixes the puzzle she want solved with fake puzzles for y she know the so

Alice reveals the puzzles and ask Tumbler to open commitments.

Alice checks the fake puzzle commitments of correct values.

Tumbler solves all the crypts the commits

cks that all the he fake then itments.

The Tumbler uses this protocol to convince Alice

**If** she learns a set of hash preimages:  
 $\text{Hash}(k_1) = h_1 \dots \text{Hash}(k_m) = h_m$

**Then** she also learns the solution to RSA Puzzle  $y$ :  
 $y^{sk} \pmod n$

under condition the running transaction is signed by  $\mathcal{T}$  and has preimages of  $h_j \forall j \in R$ .

$y, r_j \forall j \in R \rightarrow$

9. Check  $\beta_j$  unblind to  $y \forall j \in R$   
 For all  $j \in R$   
 Verify  $\beta_j = y \cdot (r_j)^{pk} \pmod N$   
 If not, abort.

10. Post transaction  $T_{\text{solve}}$   
 $T_{\text{solve}}$  contains  $k_j \forall j \in R$

Tumbler ensures that all the real puzzles have the same solution.

11. Obtain Puzzle Solution  
 For  $j \in R$ :  
 Learn  $k_j$  from  $T_{\text{solve}}$   
 Decrypt  $c_j$  to  $s_j = H^{\text{PRG}}(k_j) \oplus c_j$   
 If  $s_j$  is s.t.  $(s_j)^{pk} = \beta_j \pmod N$ ,  
 Obtain solution  $s_j/r_j \pmod N$   
 which is  $y^{sk}$ .

Alice learns the solution to  $y$  and sends it to Bob.

# Security of Puzzle-Solver-Protocol

M = size of real set →

N = size of fake set →

Alice  $\mathcal{A}$   
Input: Puzzle  $y$

1. Prepare Real Puzzles  $R$   
For  $i \in [m]$ , pick  $r_i \in \mathbb{Z}_N^*$   
 $d_i \leftarrow y \cdot (r_i)^{pk} \pmod N$

2. Prepare Fake Values  $F$   
For  $i \in [n]$ , pick  $a_i \in \mathbb{Z}^*$

- The Tumbler corrupts  $k_1, \dots, k_m$  solutions from Alice's real set
- Two parameters  $M$  and  $N$
- If the Tumbler corrupts  $> M$  solutions ... Alice will always detect cheating.

Prob of the Tumbler cheating:  
 $1/(M+N \text{ choose } M)$   
 or  
 the probability that the Tumbler correctly guesses  
 the real set of puzzles.

$M = 15, N = 285$   
 Prob of cheating =  $2^{-80}$

- If the Tumbler corrupts  $> M$  solutions:  
... Alice will always detect cheating.
- The Tumbler must corrupt exactly  $M$  solutions  
... and must only corrupt the real set.

8. Post-transaction  $T_{\text{puzzle}}$   
 $T_{\text{puzzle}}$  offers 1 bitcoin within timewindow  $tw_1$   
under condition "the fulfilling transaction is signed by  $\mathcal{T}$  and has preimages of  $h_j \forall j \in R$ ".

11. Obtain Puzzle Solution  
For  $j \in R$ :

Learn  $k_i$  from  $T_{\text{solve}}$   
Decrypt  $c_j$  to  $s_j = H^{pk}(k_j) \oplus c_j$   
If  $s_j$  is s.t.  $(s_j)^{pk} = \beta_j \pmod N$ ,  
Obtain solution  $s_j/r_j \pmod N$   
which is  $y^{sk}$ .

4. Ev  
For  $i$   
E  
E  
C  
+n  
+n  
F  
6. C  
For a  
V  
If ye  
Else  
F  
9. C  
For a  
V  
If no  
10. F  
T<sub>solve</sub>

# Puzzle-Promise-Protocol

Bob $\mathcal{B}$	Tumbler $\mathcal{T}$ . Secret input: $sk$
	1. Set up $T_{\text{escr}(\mathcal{T}, \mathcal{B})}$ Sign but do not post transaction $T_{\text{escr}(\mathcal{T}, \mathcal{B})}$ timelocked for $tw_2$ offering one bitcoin under the condition: "the fulfilling transaction must be signed under key $PK_{\mathcal{T}}^{\text{eph}}$ and under key $PK_{\mathcal{B}}$ ."
2. Prepare $\mu$ Real Unsigned $T_{\text{cash}(\mathcal{T}, \mathcal{B})}$ .	
For $i \in 1, \dots, \mu$ : Choose random pad $\rho_i \leftarrow \{0, 1\}^\lambda$ Set $T_{\text{cash}(\mathcal{T}, \mathcal{B})}^i = \text{CashOutTFormat} \parallel \rho_i$ $ht_i = H'(T_{\text{cash}}^i)$ .	$\xleftarrow{T_{\text{cash}(\mathcal{T}, \mathcal{B})}}$
3. Prepare Fake Set.	
For $i \in 1, \dots, \eta$ : Choose random pad $r_i \leftarrow \{0, 1\}^\lambda$ $ft_i = H'(\text{FakeFormat} \parallel r_i)$ .	
4. Mix Sets.	
Randomly permute $\{ft_1, \dots, ft_\eta, ht_1, \dots, ht_\mu\}$ to obtain $\{\beta_1, \dots, \beta_{\mu+\eta}\}$ Let $R$ be the indices of the $ht_i$ Let $F$ be the indices of the $ft_i$	
	$\xrightarrow{\beta_1 \dots \beta_{\mu+\eta}}$
Choose salt $\in \{0, 1\}^\lambda$ Compute: $h_R = H(\text{salt} \parallel R)$ $h_F = H(\text{salt} \parallel F)$	$\xrightarrow{h_R, h_F}$
	5. Evaluation.
	For $i = 1, \dots, \mu + \eta$ : ECDSA sign $\beta_i$ to get $\sigma_i = \text{Sig}(SK_{\mathcal{T}}^{\text{eph}}, \beta_i)$ Randomly choose $\epsilon_i \in \mathbb{Z}_N$ . Create promise $c_i = H^{\text{shk}}(\epsilon_i) \oplus \sigma_i$ Create puzzle $z_i = f_{\text{RSA}}(\epsilon_i, pk, N)$ i.e., $z_i = (\epsilon_i)^{pk} \pmod N$
	$\xleftarrow{(c_1, \sigma_1) \dots (c_{\mu+\eta}, \sigma_{\mu+\eta})}$
6. Identify Fake Set.	$\xrightarrow{R, F}$
	$\xrightarrow{r_i \forall i \in F}$
	$\xrightarrow{\text{salt}}$
8. Check Fake Set.	7. Check Fake Set.
For all $i \in F$ - Validate that $\epsilon_i < N$ - Validate RSA puzzle $z_i = (\epsilon_i)^{pk} \pmod N$ - Validate promise $c_i$ : (a) Decrypt $\sigma_i = H^{\text{pk}}(\epsilon_i) \oplus c_i$ (b) Verify $\sigma_i$ , i.e., ECDSA-Ver( $PK_{\mathcal{T}}^{\text{eph}}, H'(ft_i), \sigma_i$ ) = 1	Check $h_R = H(\text{salt} \parallel R)$ and $h_F = H(\text{salt} \parallel F)$ For all $i \in F$ : verify $\beta_i = H'(\text{FakeFormat} \parallel r_i)$ .
Abort if any check fails	Abort if any check fails
	$\xleftarrow{\epsilon_i \forall i \in F}$
10. Quotient Test.	9. Prepare Quotients.
For $R = \{j_1, \dots, j_\mu\}$ check equalities: $z_{j_2} = z_{j_1} \cdot (q_2)^{pk} \pmod N$ ... $z_{j_\mu} = z_{j_{\mu-1}} \cdot (q_\mu)^{pk} \pmod N$	For $R = \{j_1, \dots, j_\mu\}$ : set $q_2 = \frac{\epsilon_{j_2}}{\epsilon_{j_1}}, \dots, q_\mu = \frac{\epsilon_{j_\mu}}{\epsilon_{j_{\mu-1}}}$
Abort if any check fails	$\xleftarrow{q_2, \dots, q_\mu}$
12. Begin Payment Phase.	11. Post transaction $T_{\text{escr}(\mathcal{T}, \mathcal{B})}$ on blockchain
Set $z = z_{j_1}$ . Send $\bar{z} = z \cdot (r)^{pk}$ to Payer $\mathcal{A}$	

# TumbleBit: Roadmap

## Phase 1: Code Safety and Testing

- ❑ Move as much code as possible into python for improved memory safety.
- ❑ Modularize code to allow our core protocol to be used in other settings.
- ❑ Replace openssl-ECDSA with libsecp256k1.

## Phase 2: Server Features

- ❑ Payment Hub support.
- ❑ Misbehavior reactive server and client.
- ❑ Session Management and parallelization.
- ❑ TOR integration.
- ❑ Standardized REST Interface.

## Phase 3: Usability and Wallets

- ❑ Wallet Prototype.
- ❑ Classic Tumbler Wallet integration.
- ❑ Payment Hub Wallet integration.
- ❑ Wallet to wallet demo.

## Phase 4: Operational Concerns

- ❑ Monitoring.
- ❑ Audit and test at-scale deployment.
- ❑ Assess, test and mitigate server compromise risks.
- ❑ Release ops guide.

## Phase 5: Alpha Release

- ❑ User guides and documentation.
- ❑ Wallet binaries.

# Puzzle-Solver-Protocol

Alice $\mathcal{A}$	Tumbler $\mathcal{T}$
Input: Puzzle $y$	Secret input: $sk$

### 1. Prepare Real Puzzles $R$

For  $i \in [m]$ , pick  $r_i \in \mathbb{Z}_N^*$   
 $d_i \leftarrow y \cdot (r_i)^{pk} \pmod N$

### 2. Prepare Fake Values $F$

For  $i \in [n]$ , pick  $\rho_i \in \mathbb{Z}_N^*$   
 $\delta_i \leftarrow (\rho_i)^{pk} \pmod N$

### 3. Mix Sets.

Randomly permute

$\{d_1 \dots d_m, \delta_1 \dots \delta_n\}$

to  $\{\beta_1 \dots \beta_{m+n}\}$

Let  $R$  be the indices of the  $d_i$

Let  $F$  be the indices of the  $\delta_i$

$\xrightarrow{\beta_1 \dots \beta_{m+n}}$

### 4. Evaluation

For  $i = 1 \dots m+n$

Evaluate  $\beta_i$ :  $s_i = \beta_i^{sk} \pmod N$

Encrypt the result  $s_i$ :

– Choose random  $k_i \in \{0, 1\}^{\lambda_1}$

–  $c_i = H^{prg}(k_i) \oplus s_i$

Commit to the keys:  $h_i = H(k_i)$

$\xleftarrow{c_1, \dots, c_{m+n}}$

$\xleftarrow{h_1, \dots, h_{m+n}}$

$\xrightarrow{F, \rho_i \forall i \in F}$

### 5. Identify Fake Set $F$

### 7. Check Fake Set $F$

For all  $i \in F$ ,

Verify that  $h_i = H(k_i)$

Decrypt  $s_i = H^{prg}(k_i) \oplus c_i$

Verify  $(s_i)^{pk} = (\rho_i) \pmod N$

Abort if any check fails.

$\xleftarrow{k_i \forall i \in F}$

### 8. Post transaction $T_{\text{puzzle}}$

$T_{\text{puzzle}}$  offers 1 bitcoin within timewindow  $tw_1$   
 under condition “the fulfilling transaction is  
 signed by  $\mathcal{T}$  and has preimages of  $h_j \forall j \in R$ ”.

$\xrightarrow{y, r_j \forall j \in R}$

### 6. Check Fake Set $F$

For all  $i \in F$ :

Verify  $\beta_i = (\rho_i)^{pk} \pmod N$ ,

If yes, reveal  $k_i \forall i \in [F]$ .

Else abort.

### 9. Check $\beta_j$ unblind to $y \forall j \in R$

For all  $j \in R$

Verify  $\beta_j = y \cdot (r_j)^{pk} \pmod N$

If not, abort.

### 10. Post transaction $T_{\text{solve}}$

$T_{\text{solve}}$  contains  $k_j \forall j \in R$

### 11. Obtain Puzzle Solution

For  $j \in R$ :

Learn  $k_i$  from  $T_{\text{solve}}$

Decrypt  $c_j$  to  $s_j = H^{prg}(k_j) \oplus c_j$

If  $s_j$  is s.t.  $(s_j)^{pk} = \beta_j \pmod N$ ,

Obtain solution  $s_j/r_j \pmod N$

which is  $y^{sk}$ .

# TumbleBit: Paying with RSA-Puzzles



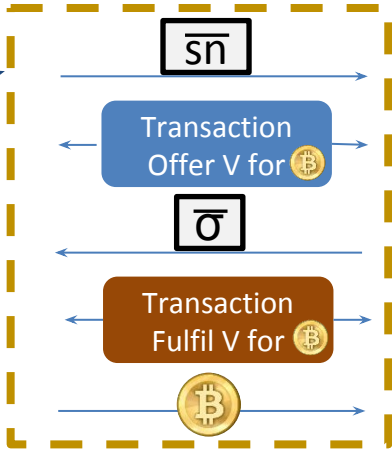
$$z = \epsilon^{pk} \text{ mod } N$$

$$c = \text{Enc}(\epsilon, \sigma)$$

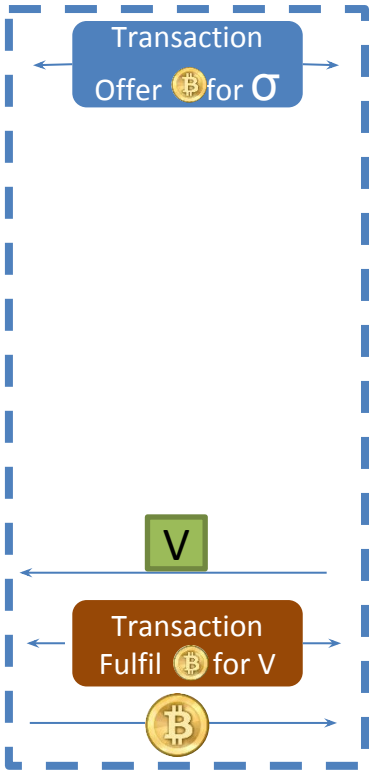
$(z, c)$

$\epsilon^*$

Fair exchange 1:  
A: Gives 1 bitcoin  
A: Gets 1 voucher



Fair exchange 1:  
B: Gives  $\sigma$   
B: Gets 1 bitcoin



# Bitcoin faces three technology challenges:

## 1. **Scaling transaction velocity (speed of payments):**

- Bitcoin transaction confirmations is ~10 min,  
... occasionally an hour or more.
- No confirmation = no double spending protection.

## 2. **Scaling transaction volume (max # of payments):**

- “Bitcoin achieves 7 transactions/sec maximum throughput ...[Visa] processes 2000 transaction/sec on average, with a peak rate of 56,000 transactions/sec”[1]
- To compete with mainstream payment processors  
... Bitcoin needs to support much higher transaction volume.
- Limiting factor here is space in the blockchain.

## 3. **Anonymity and user privacy:**

- Bitcoin transactions are saved in the blockchain  
... creating an eternal public record of payment history.

[1]: ‘On Scaling Decentralized Blockchains (A Position Paper)’ Croman, et al.

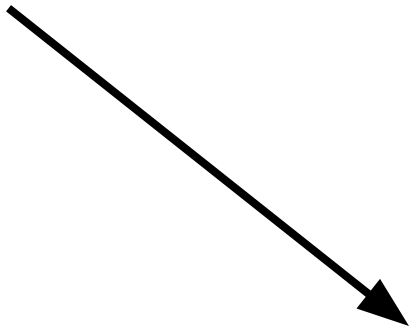
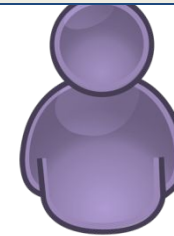


# Paying with RSA-Puzzles



Tumbler

Transaction 1:  
Bob can claim 1 Bitcoin  
if he knows a



## 10. Privacy

The traditional banking model achieves a level of privacy by limiting access to information to the parties involved and the trusted third party. The necessity to announce all transactions publicly precludes this method, but privacy can still be maintained by breaking the flow of information in another place: by keeping public keys anonymous. The public can see that someone is sending an amount to someone else, but without information linking the transaction to anyone. This is similar to the level of information released by stock exchanges, where the time and size of individual trades, the "tape", is made public, but without telling who the parties were.

*Satoshi Nakamoto, 2008*

**Bitcoin offers privacy—as long as you don't cash out or spend it**

### **A Fistful of Bitcoins: Characterizing Payments Among Men with No Names**

Sarah Meiklejohn Marjori Pomarole Grant Jordan  
Levchenko Damon McCoy<sup>†</sup> Geoffrey M. Voelker Stefan Savage  
University of California, San Diego George Mason University<sup>†</sup>

### **Quantitative Analysis of the Full Bitcoin Transaction Graph**

Dorit Ron and Adi Shamir

Department of Computer Science and Applied Mathematics,  
The Weizmann Institute of Science, Israel  
{dorit.ron, adi.shamir}@weizmann.ac.il

### **Evaluating User Privacy in Bitcoin**

Elli Androulaki<sup>1</sup>, Ghassan O. Karame<sup>2</sup>, Marc Roeschlin<sup>1</sup>,  
Tobias Scherer<sup>1</sup>, and Srdjan Capkun<sup>1</sup>

or the public ledger that records bit  
bitcoins move from one person to a  
alphanumeric addresses.

# Introduction

## Privacy:

- Bitcoin is not anonymous
- Payment history saved in an eternal public record

## Transaction velocity:

- Transactions confirmed on the blockchain
- No confirmation = double spending possible
- Avg confirmation time is ~10 min

## Transaction volume: Max # payments

- Bitcoin: 7 Tx/sec max throughput[1]
- Visa: (avg) 2000 Tx/sec[1]
- Visa: (peak) 56,000 Tx/sec[1]
- Limiting factor is space in the blockchain

[1]: 'On Scaling Decentralized Blockchains (A Position Paper)' Croman, et al.

# Introduction

## Technical challenges facing Bitcoin:

### Privacy:

- Bitcoin is not anonymous
- Payment history saved in an eternal public record

### Transaction velocity:

- Transactions confirmed on the blockchain
- No confirmation = double spending possible
- Avg confirmation time is ~10 min

### Transaction volume: Max # payments

- Bitcoin: 7 Tx/sec max throughput[1]
- Visa: (avg) 2000 Tx/sec[1]
- Visa: (peak) 56,000 Tx/sec[1]
- Limiting factor is space in the blockchain

[1]: 'On Scaling Decentralized Blockchains (A Position Paper)' Croman, et al.

# TumbleBit: scalability and payment privacy.

- ✓ **1. Scaling transaction velocity (speed of payments):**
  - TumbleBit as a payment hub can make payments in seconds.
- ✓ **2. Scaling transaction volume (max # of payments):**
  - Payment hubs allow many payments to one party to be aggregated into two on-blockchain transactions.
  - These payments don't need to be stored or validated on the blockchain.
- ✓ **3. Anonymity and payment privacy:**
  - TumbleBit provides payment privacy via unlinkability.

In this talk I am only going to tell you about how TumbleBit provides trustless payment privacy.